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Tuning infrared phonon anomalies in optical conductivity of bilayer graphene: matching theory and experiments

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Phonon features in optical spectroscopy

analysis of phonon peak features in optics

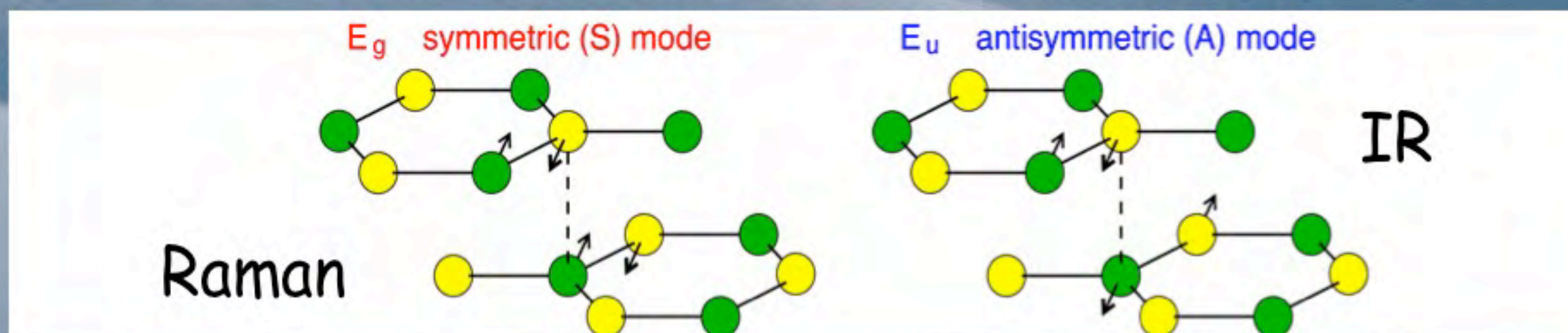
- characterization (N. layers, doping, disorder...)
- revealing of underlying many-body (el-ph) interactions
- investigation fundamental physics (Kohn anomalies, nonadiabaticity)

so far, most works mainly done using Raman spectroscopy

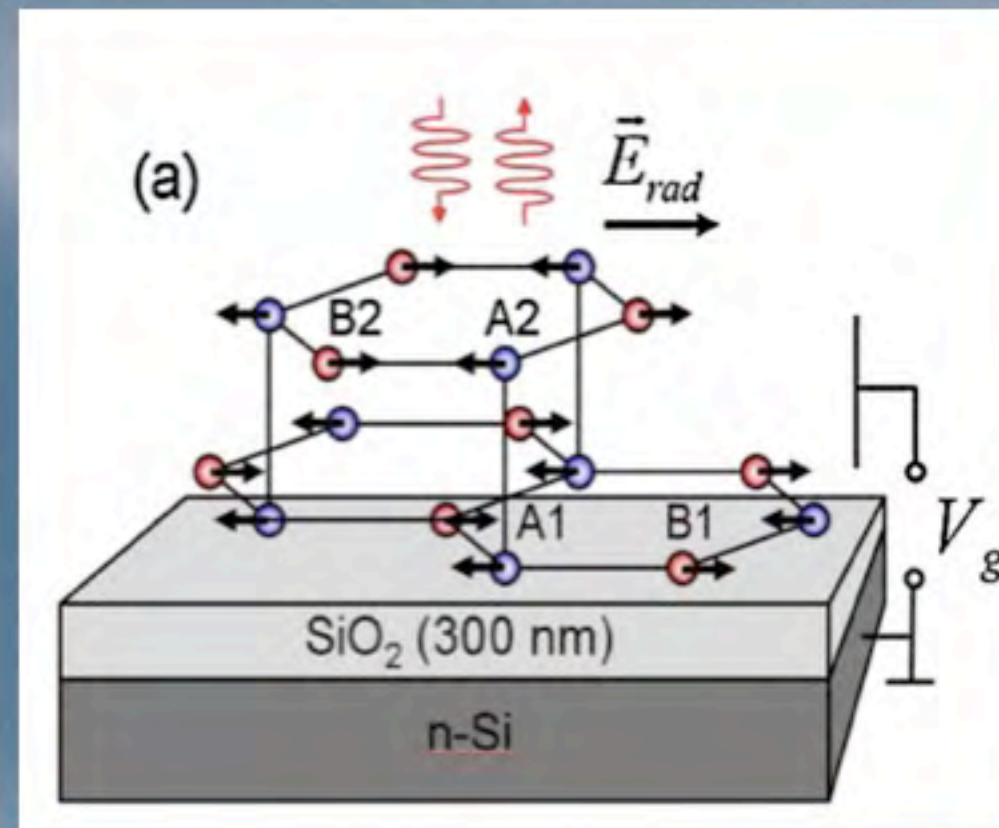
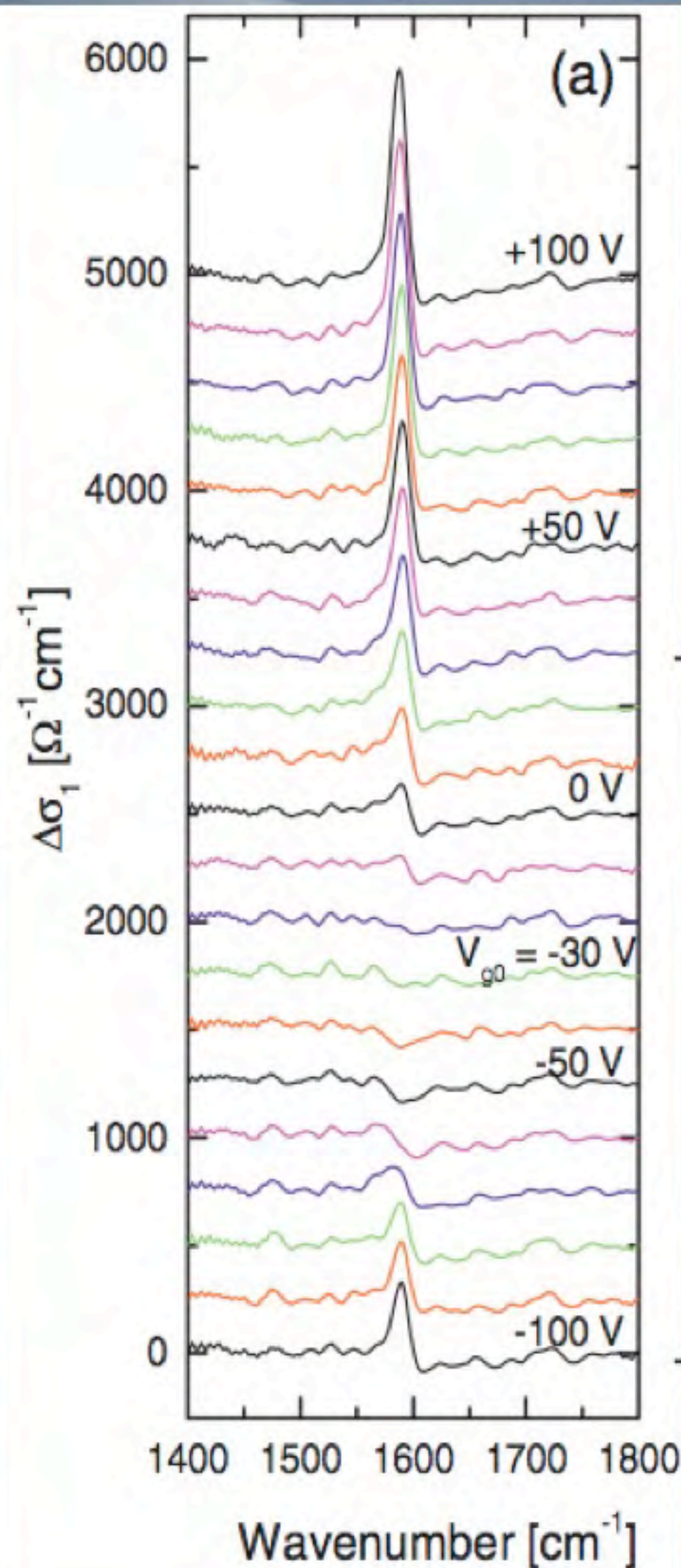
- phonon frequencies and linewidths
- absolute intensity G peaks not doping dependent

phonon features in infrared spectroscopy

- complementary information (different phonon symmetry)
- much sensible to n. layers/stacking (absent in 1 layer)
- further suitable properties (absolute intensity + lineshape asymmetry)

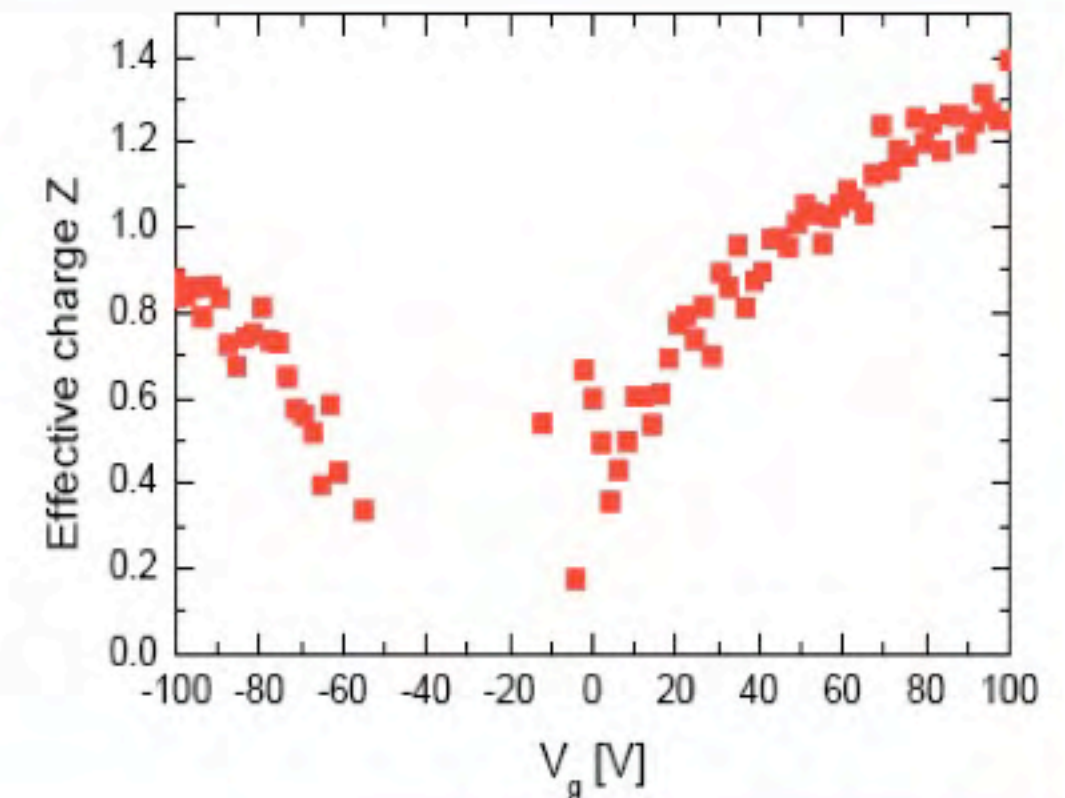
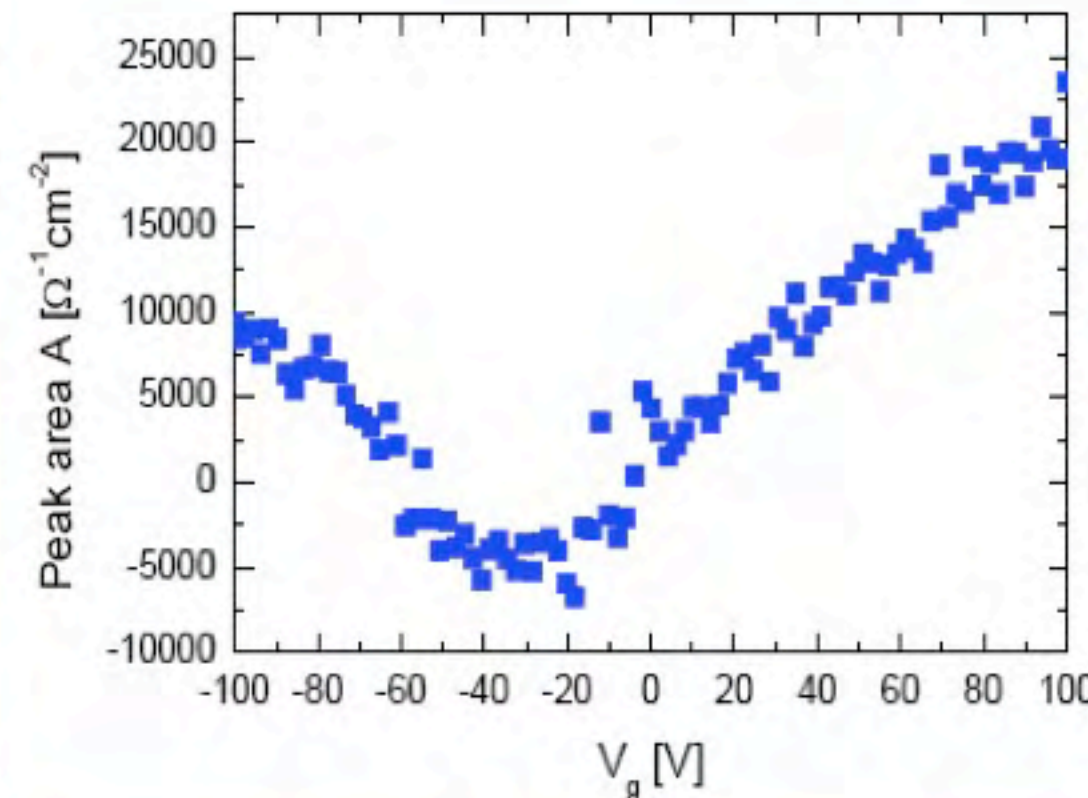


Exp. results: Geneve group



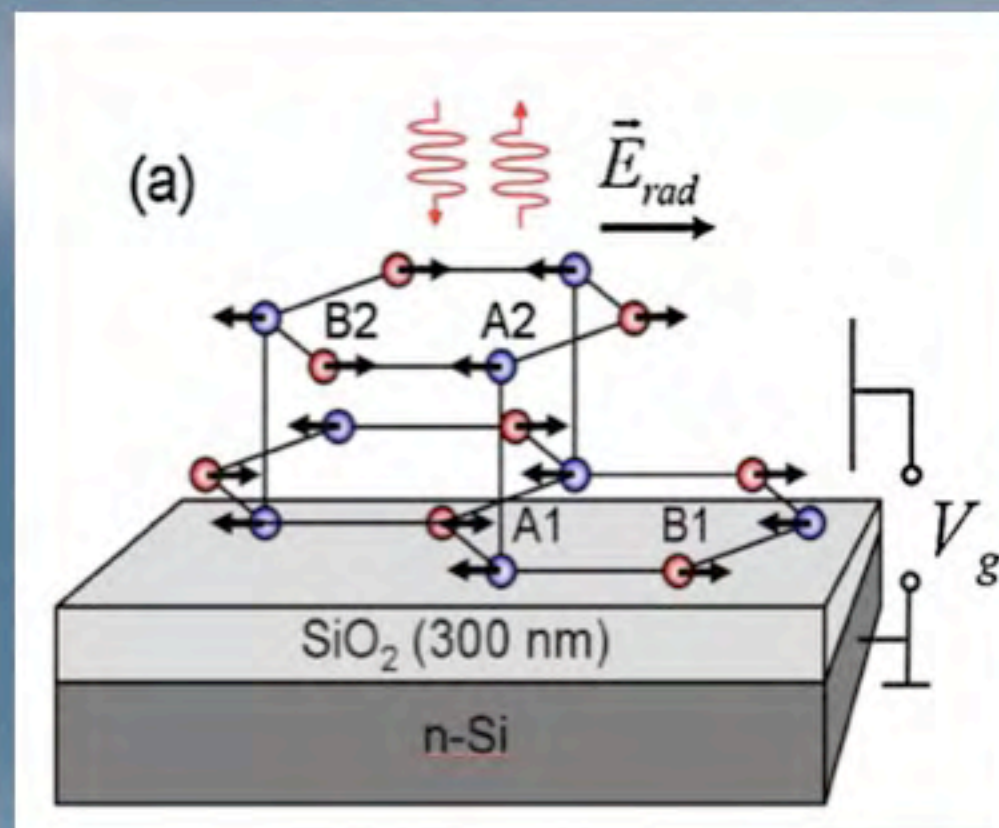
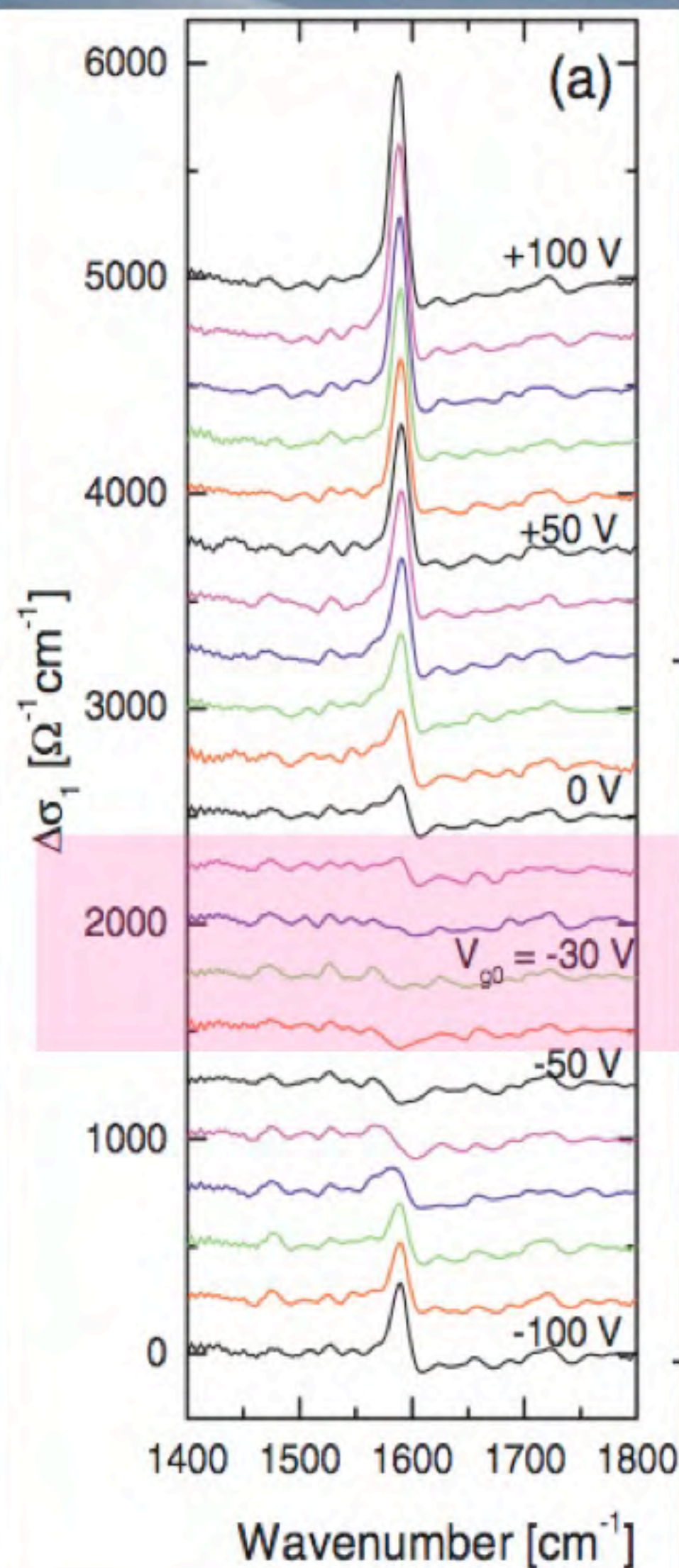
bilayer graphene

tunable phonon
peak intensity



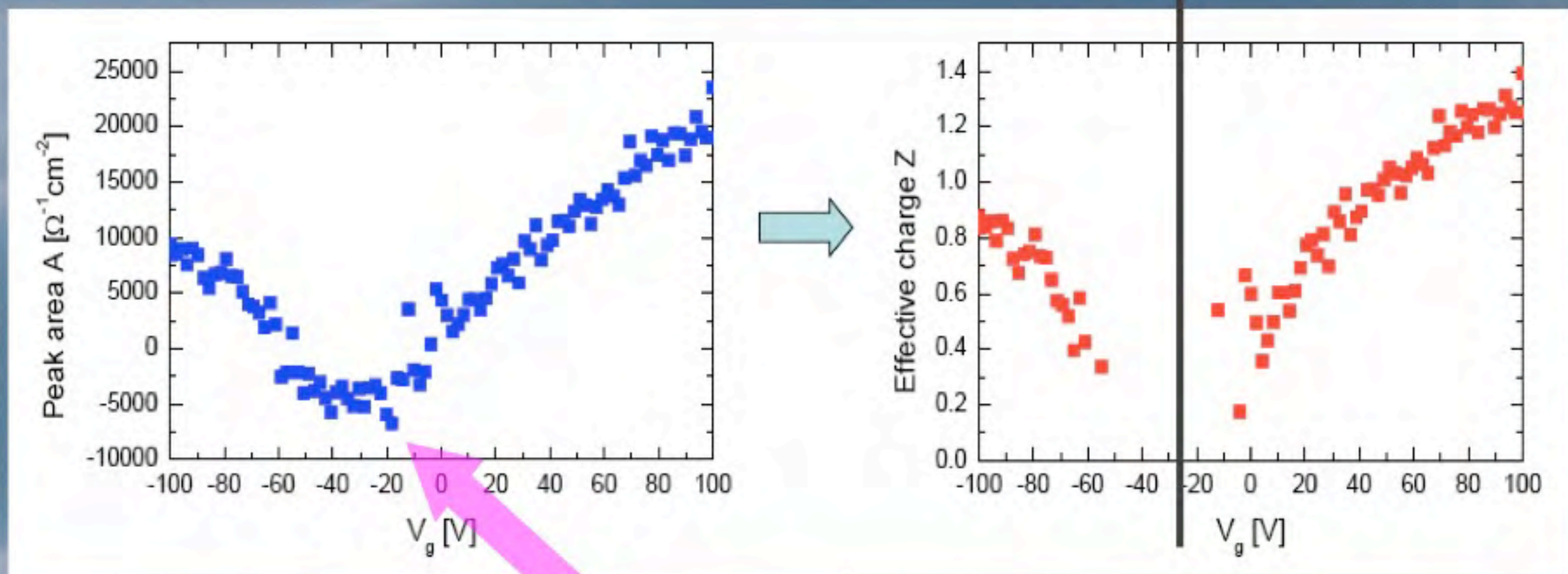
$Z_{\max} \sim 1.2!!$ huge!
as large as 1 electron over $N=4$ (sp^3) !!

Exp. results: Geneve group



tunable phonon
peak intensity

neutrality point (NP) $n=0$



also problem: negative peak area...
Z not defined...?

Exp. results: Geneve group

● four independent parameter fit

$$\sigma'(\omega) - \sigma'_{BG}(\omega) = \frac{\omega_p^2}{4\pi\Gamma} \frac{q^2 - 1 - 2qz}{q^2(z^2 + 1)}$$

$$\left[z = \frac{\omega - \omega_0}{\Gamma} \right]$$

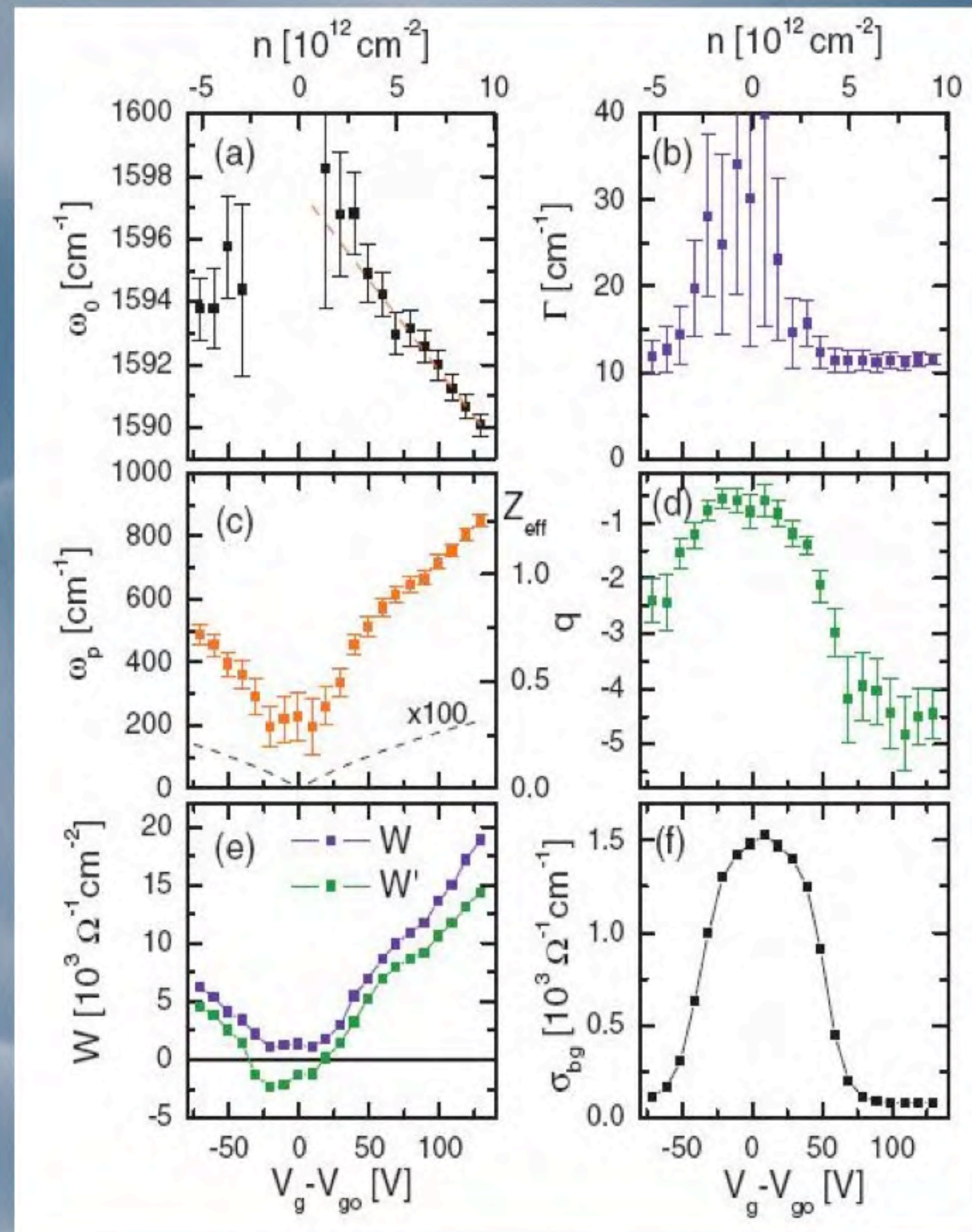
- ω_0 : phonon frequency
- Γ : phonon linewidth
- ω_p : related to intensity
- q : Fano asymmetry

$$W' = \frac{\omega_p^2}{8} \left(1 - \frac{1}{q^2} \right)$$

$$W = \frac{\omega_p^2}{8}$$



"bare" intensity (in the absence of Fano)

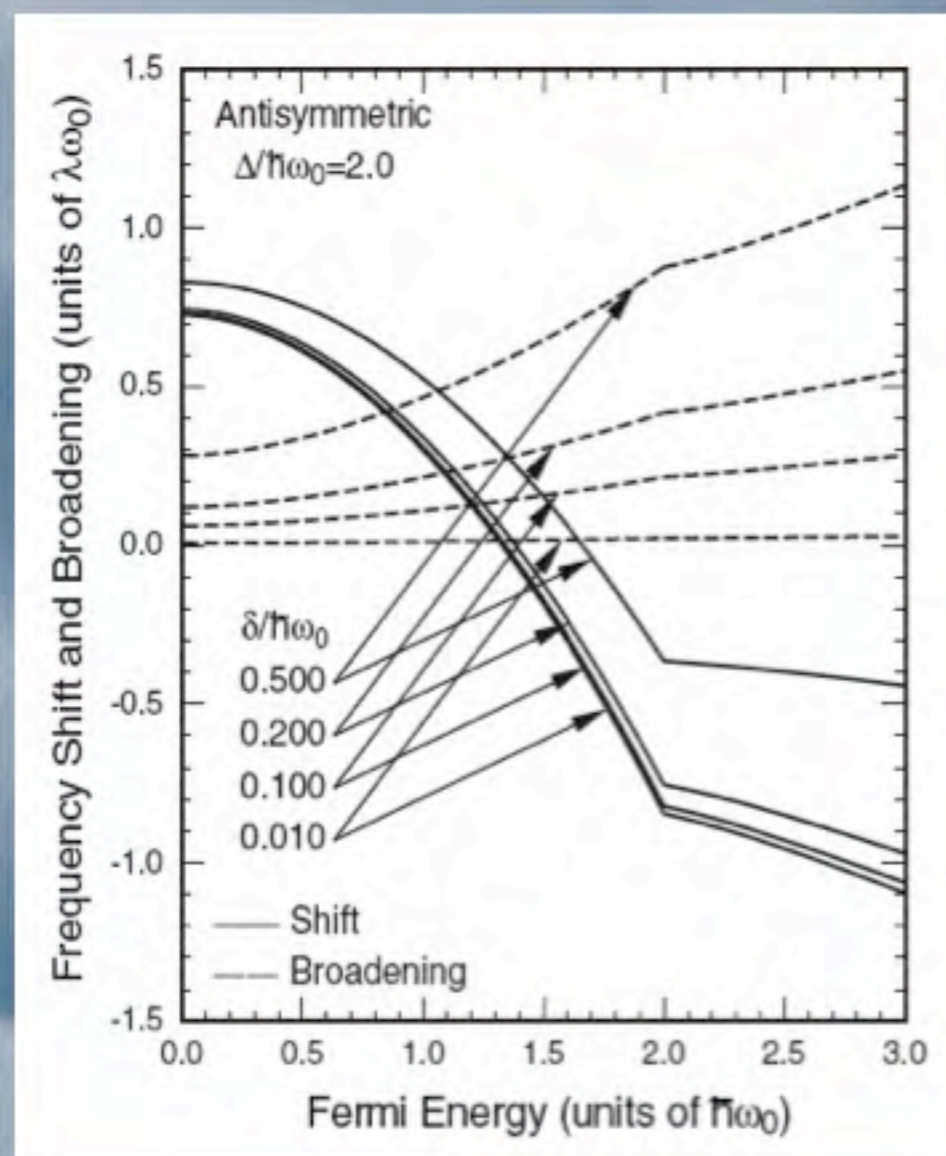


Exp. results: Geneve group

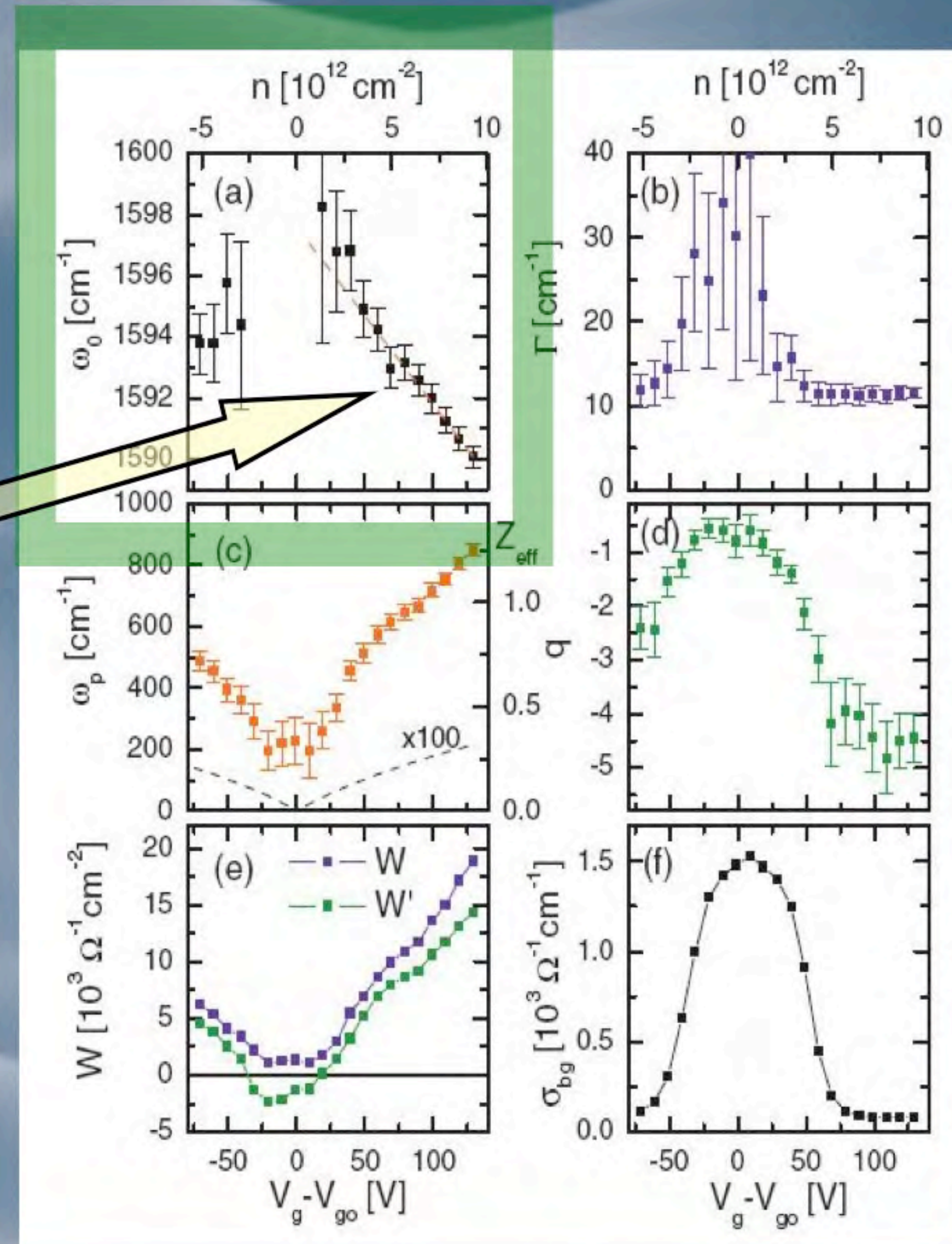
- phonon softening with doping:
ok with LDA and TB theory

~~E_g (S) mode~~

E_u (A) mode



T Ando, JPSJ 76, 104711 (2007)

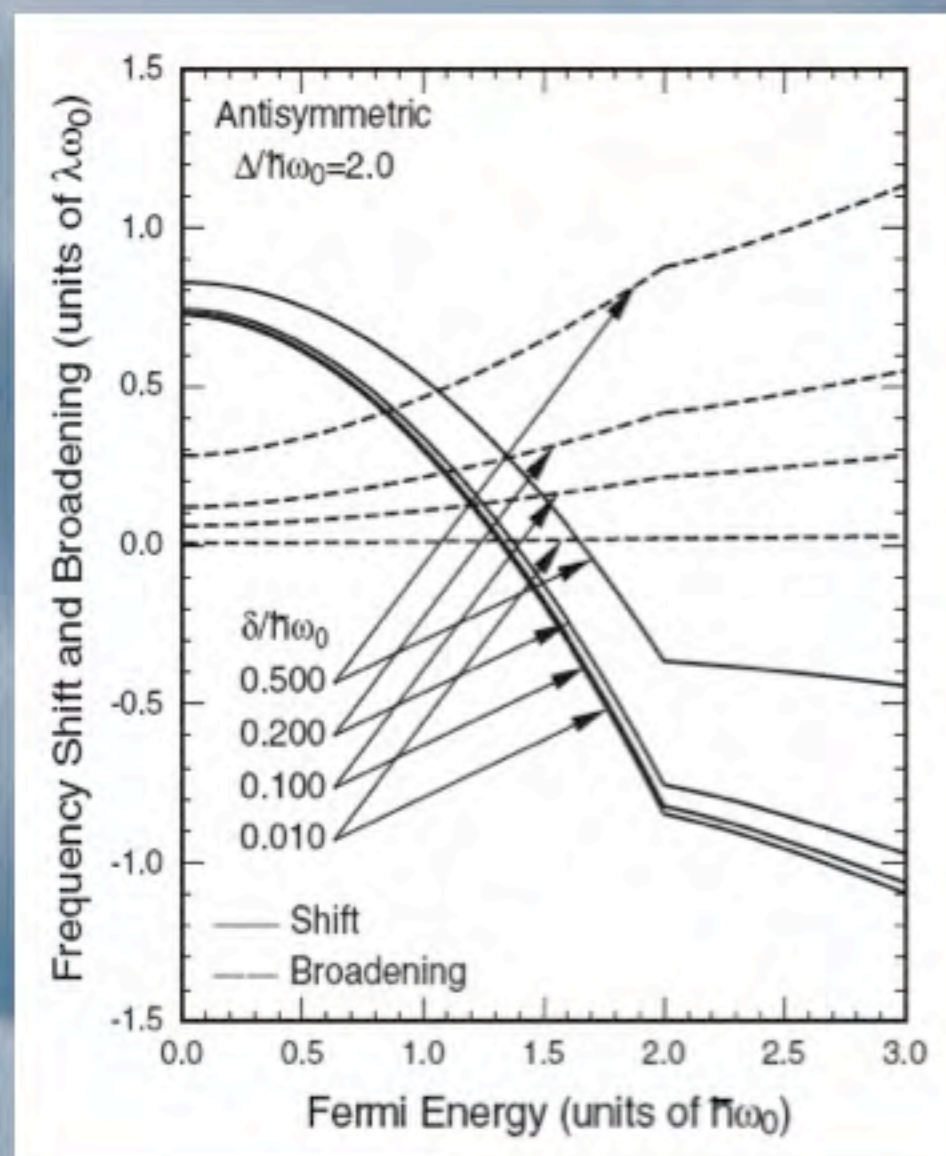


AB Kuzmenko et al, PRL 103, 116804 (2009)

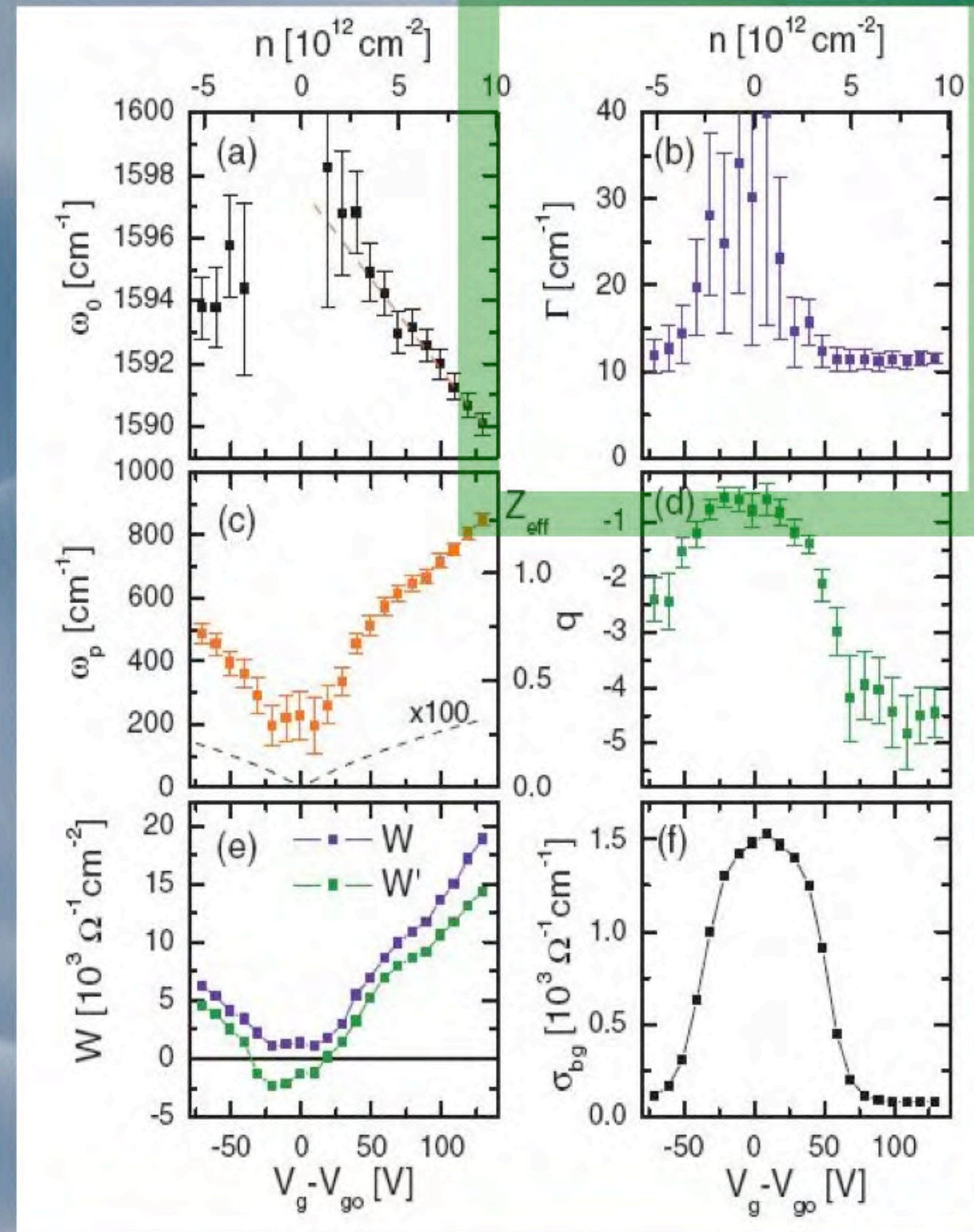
Exp. results: Geneve group

- phonon softening with doping: ok with LDA and TB theory
- phonon linewidth: strong increase at NP: why??

E_u (A) mode?



T Ando, JPSJ 76, 104711 (2007)

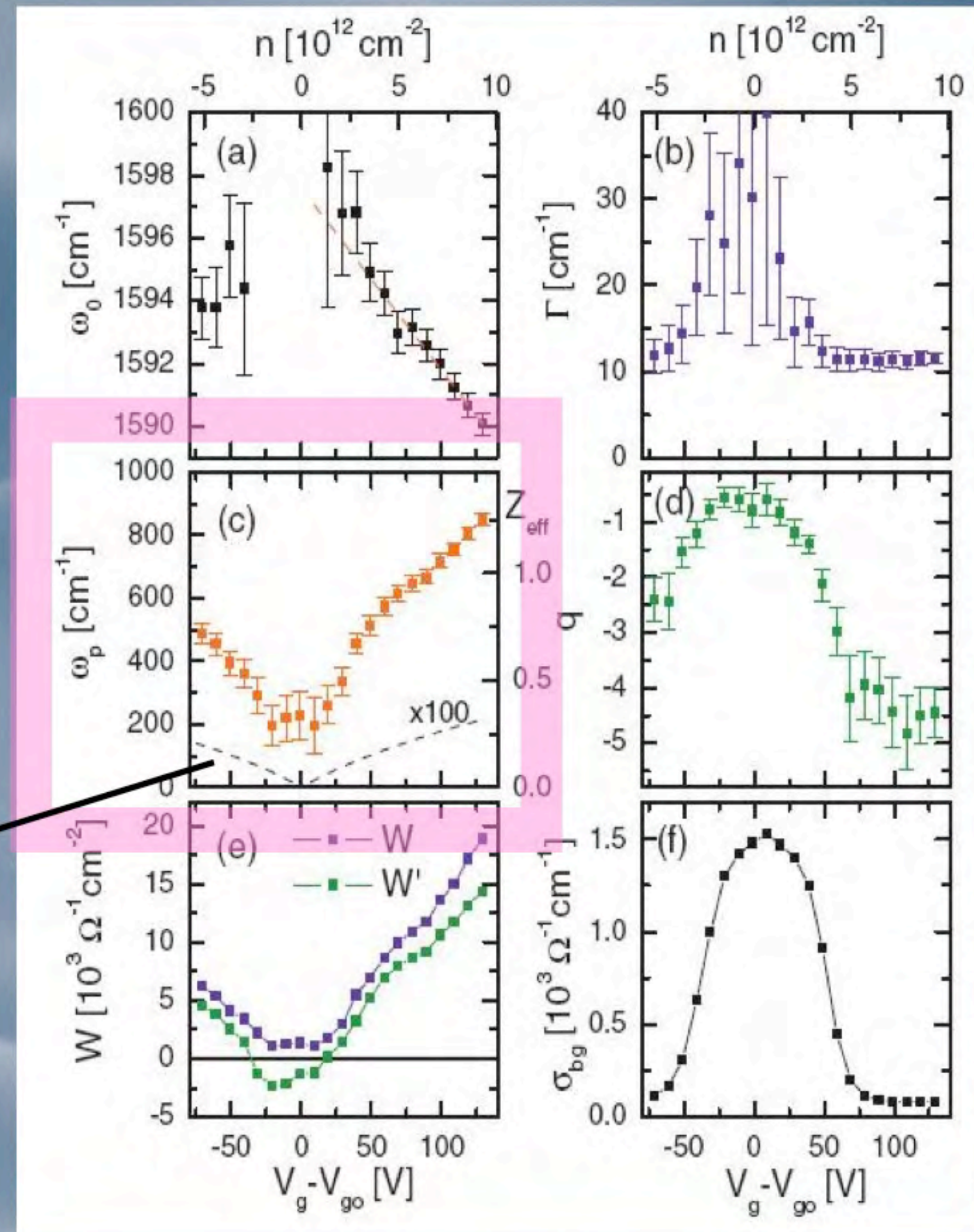


AB Kuzmenko et al, PRL 103, 116804 (2009)

Exp. results: Geneve group

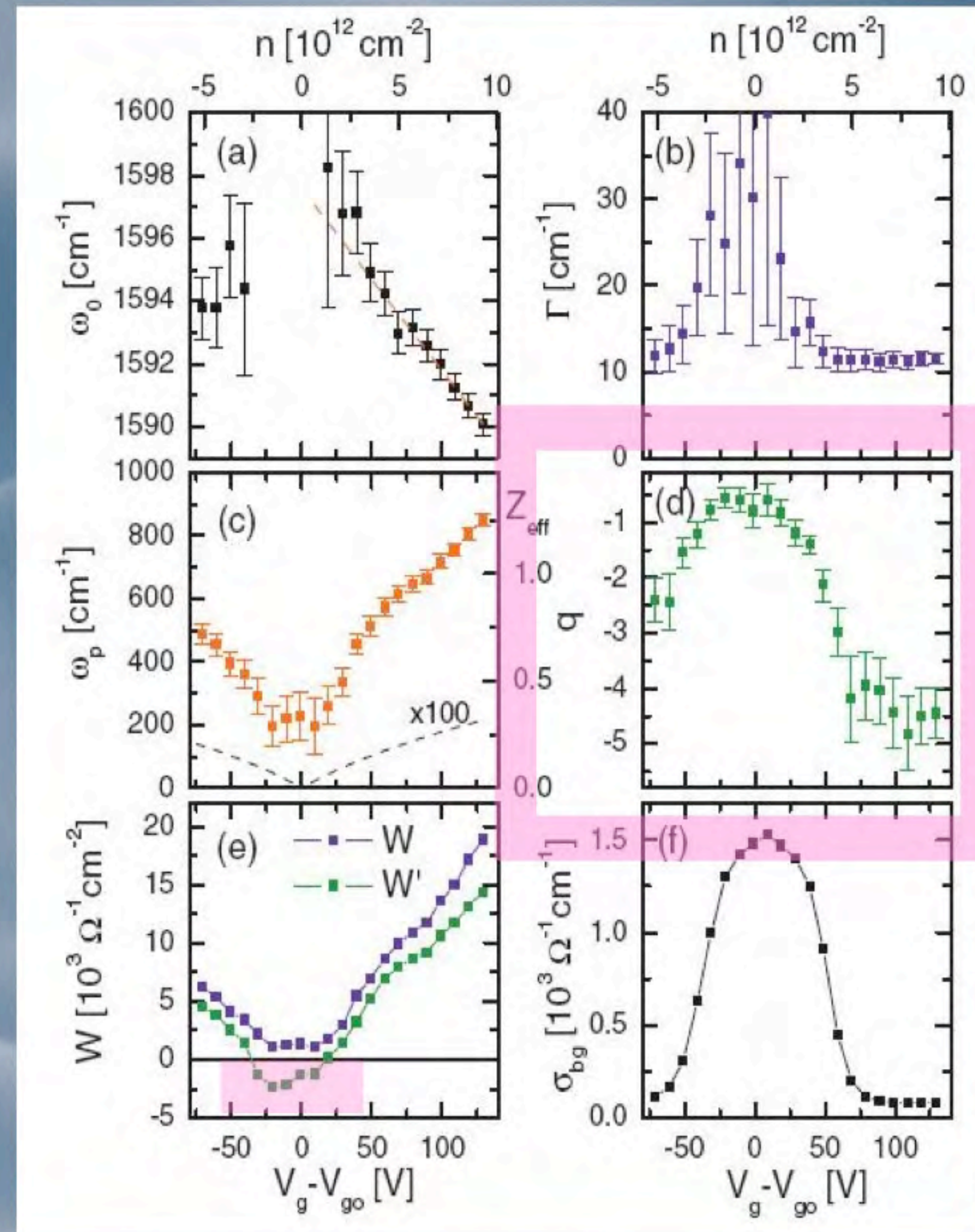
- phonon softening with doping: ok with LDA and TB theory
- phonon linewidth: not clear, but poor exp. resolution
- linear dependence of bare intensity with doping: where from? why so huge Z ?

NB: tight-binding calculations

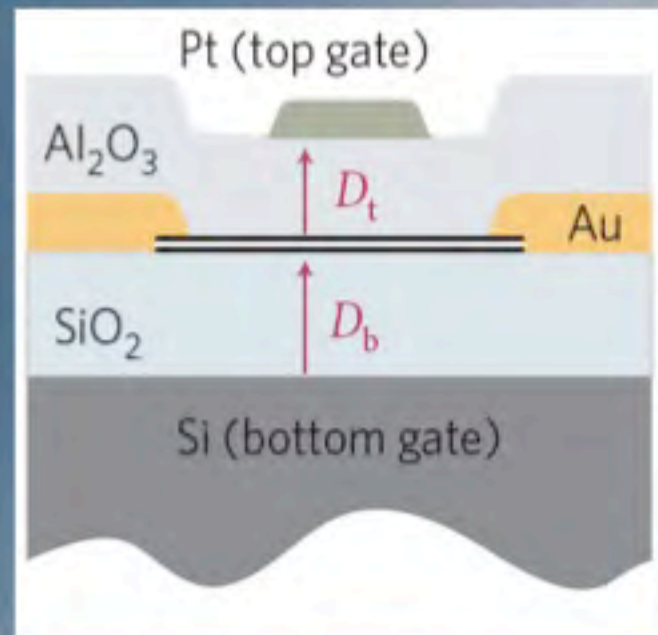


Exp. results: Geneve group

- phonon softening with doping: ok with LDA and tB theory
- phonon linewidth: not clear, but poor exp. resolution
- linear dependence of bare intensity with doping: where from? why so huge Z ?
- Fano asymmetry: where from? related to el. optical background? points out finite intensity at $n=0$...!



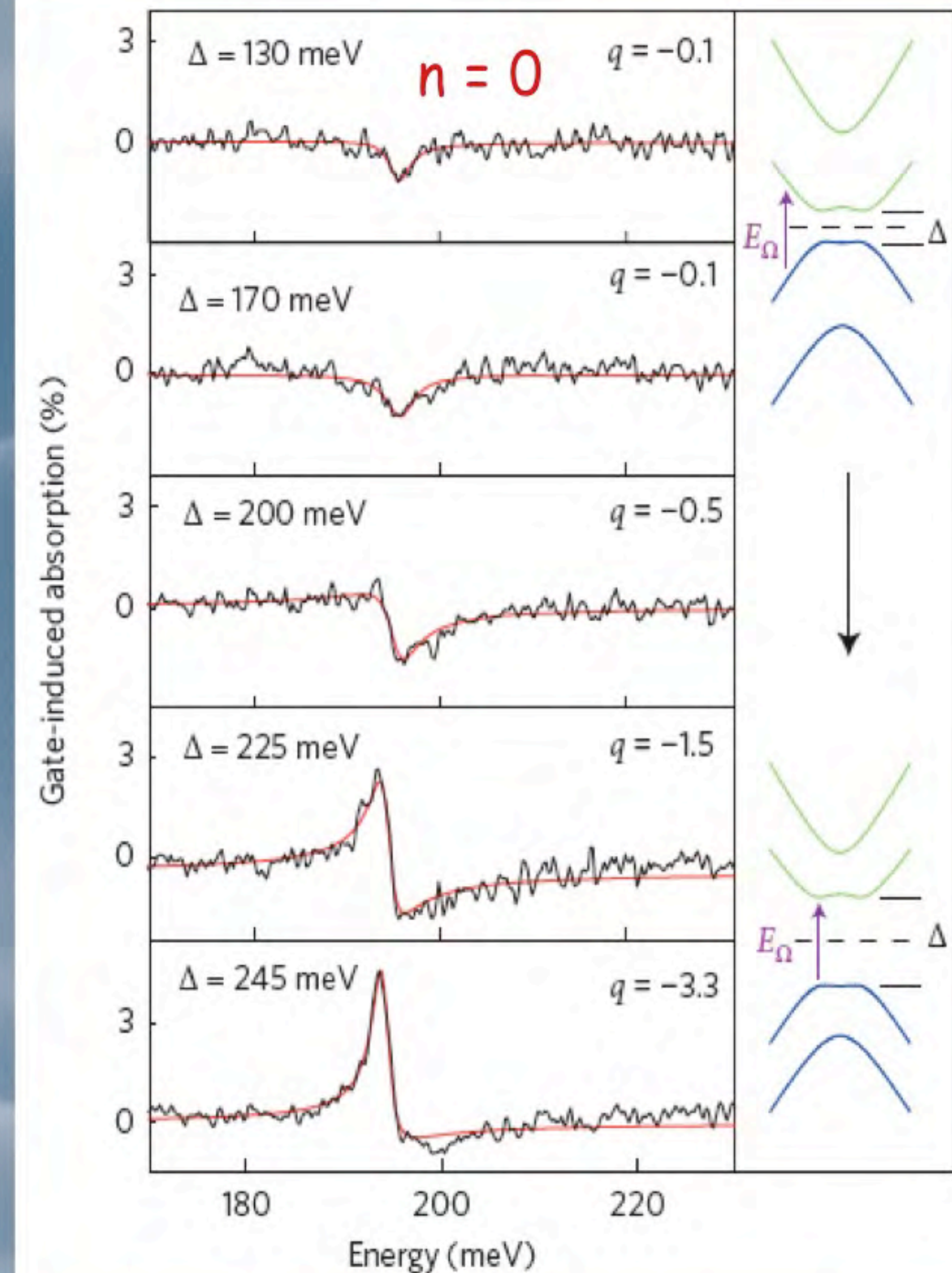
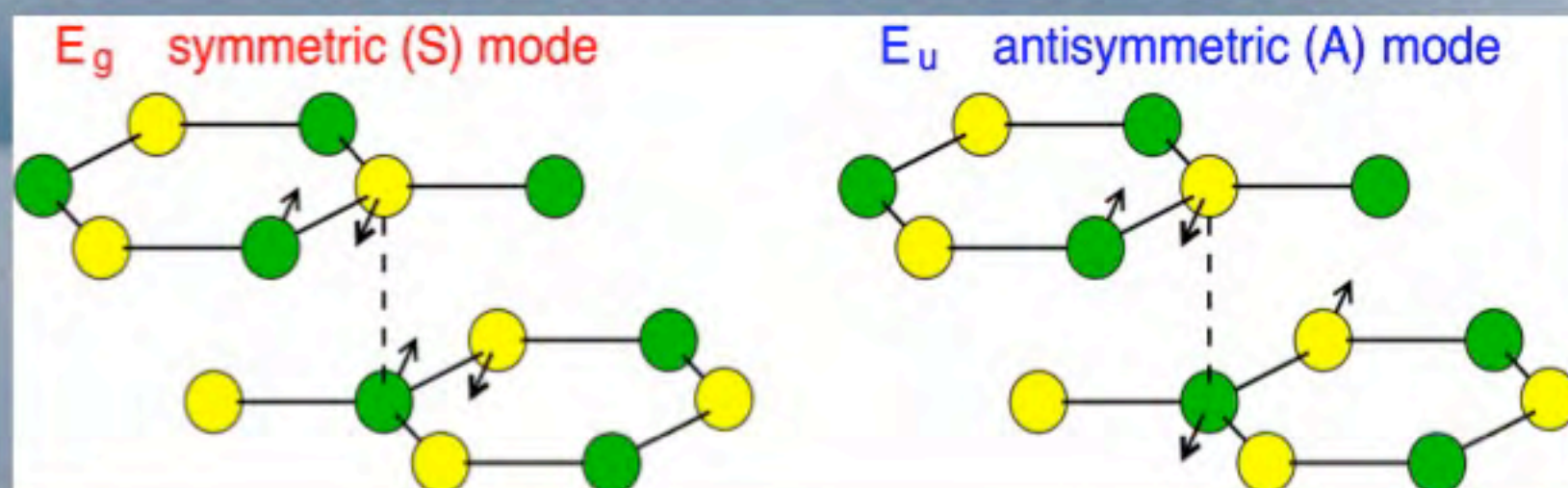
Exp. results: Berkeley group



double-gated device
possible tuning doping and Δ in independent way

- $n = 0$ and $\Delta \neq 0$: negative peak like us
- Fano effect as a function of Δ
- they attribute origin of negative peak at $n = 0$ to E_g (S) (Raman-active) mode

(S allowed by symmetry in IR when $\Delta \neq 0$)



Towards an unifying theory

- what rules the IR phonon intensity of the A mode??
(graphenes: monoatomic systems, no intrinsic dipole...)
- what rules the IR phonon intensity of the S mode??
- what the origin of the Fano lineshape of both modes and why their different Fano phenomenology??
- is it possible to find a common theoretical background explaining all these features?
- need of a quantitative theory to be predictable

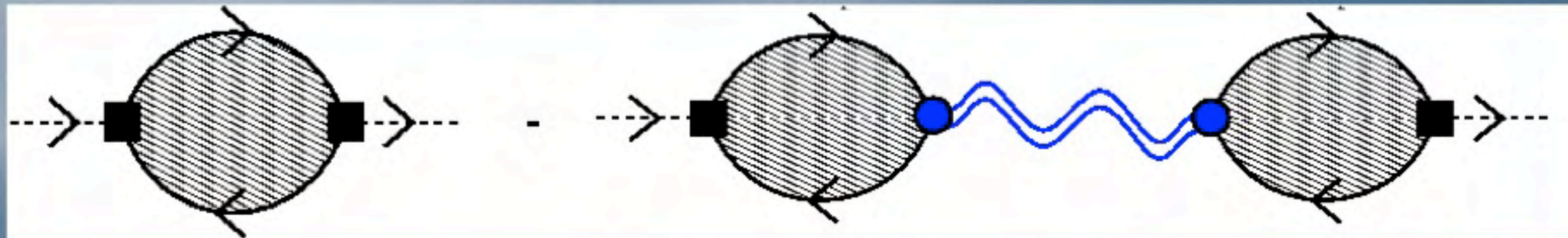
Rice (Michael) theory

applied to organic materials, fullerenes, molecular crystals...

electronic polarizability provides finite IR intensity to phonon modes allowed but otherwise not active

$$\sigma_{el}(\omega) = -i\omega\chi(\omega) \quad \chi: \text{el. polarizability (interband transitions)}$$

χ : electronic background + el-ph interaction



$$\sigma_{tot}(\omega) = -i\omega \left[\chi(\omega) + \lambda_v x \chi(\omega) \chi(\omega) D_{ph}(\omega) \right]$$

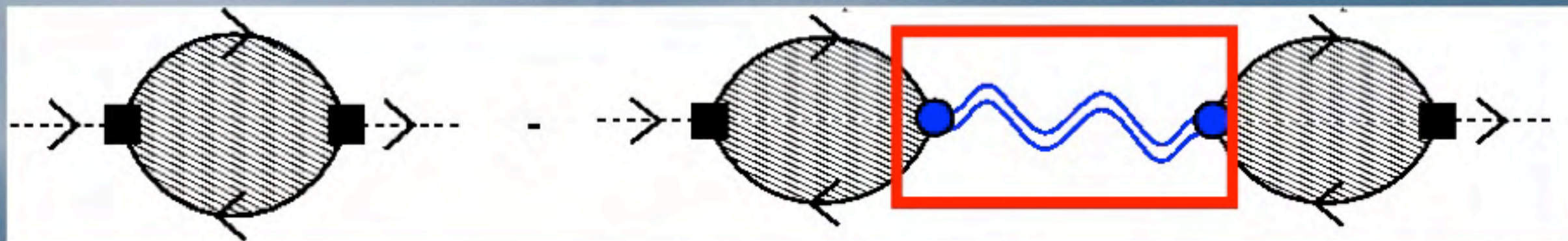
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phonon resonance

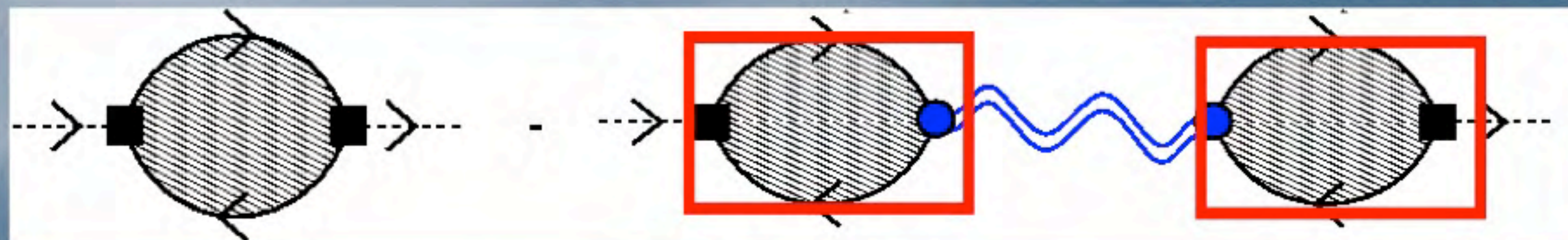
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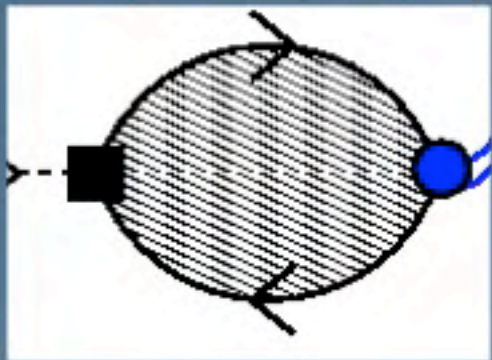
current/
electron-phonon
response function

$$\sigma_{tot}(\omega) = -i\omega \left[\chi(\omega) + \lambda_{\nu} \chi(\omega) \chi(\omega) D_{ph}(\omega) \right]$$

intensity ruled by the current/electron-phonon response function

Rice theory in bilayer graphene

Rice theory: in its original application: semiconductors



χ : **real** function ($\propto$ doping) tuning the phonon intensity

effective theory:



interesting peculiarities of bilayer graphene:



zero gap semiconductor:

low energy interband transitions $\rightarrow \chi$: complex quantity

$\rightarrow$ Fano asymmetry



tunable charged-phonon effects controlled by external voltage biases (doping and gap)

Fano-Rice theory in bilayer graphene

- interband transitions at low energy:

$$\chi_{jA} = \text{Re}\chi_{jA} + i\text{Im}\chi_{jA}$$

(gapped systems: $\text{Im}\chi_{jA} = 0$)

$$D_{AA}(\omega) = \frac{1}{\omega - \omega_A + i\Gamma_A}$$

$$\sigma'_{ep}(\omega)\Big|_{\omega \approx \omega_A} = \frac{2[\chi'_{jA}(\omega_A)]^2}{\omega_A \Gamma_A} \frac{q_A^2 - 1 + 2zq_A}{q_A^2(1 + z^2)} \quad q_A = -\frac{\chi'_{jA}(\omega_A)}{\chi''_{jA}(\omega_A)}$$

Fano formula!



Fano and charged-phonon effects same origin!



it permits a microscopical identification

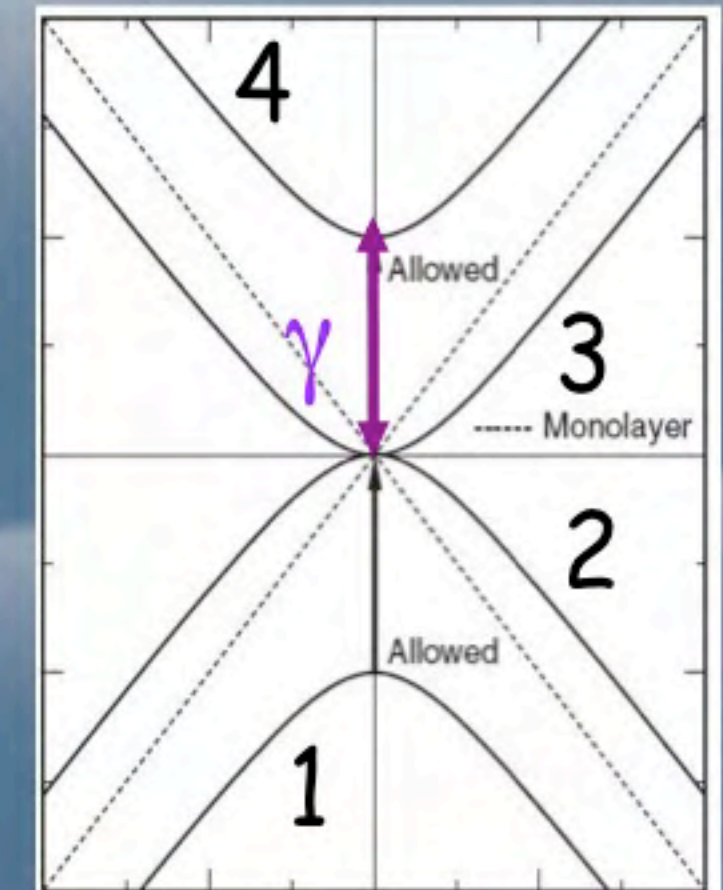
Phonon intensity in bilayer graphene

● Step by step analysis: gating induces doping but not E_z

● in this case low-energy transitions between 2 and 3

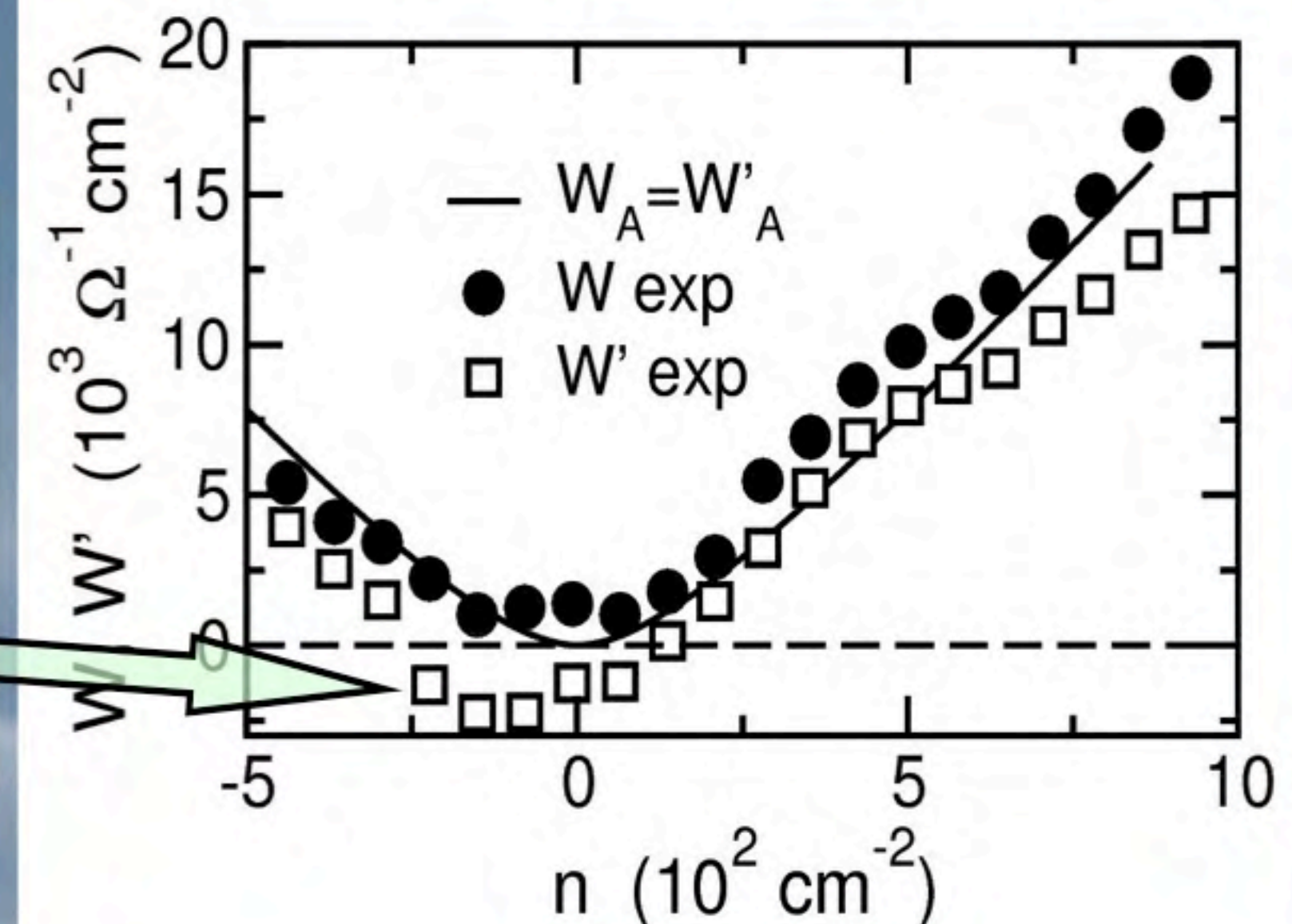
system like a gapped semiconductor

$\text{Im}\chi = 0 \rightarrow$ **no** Fano effect



doping dependence of ω -integrated area W'
perfectly reproduced

what about W_A ?
negative area?



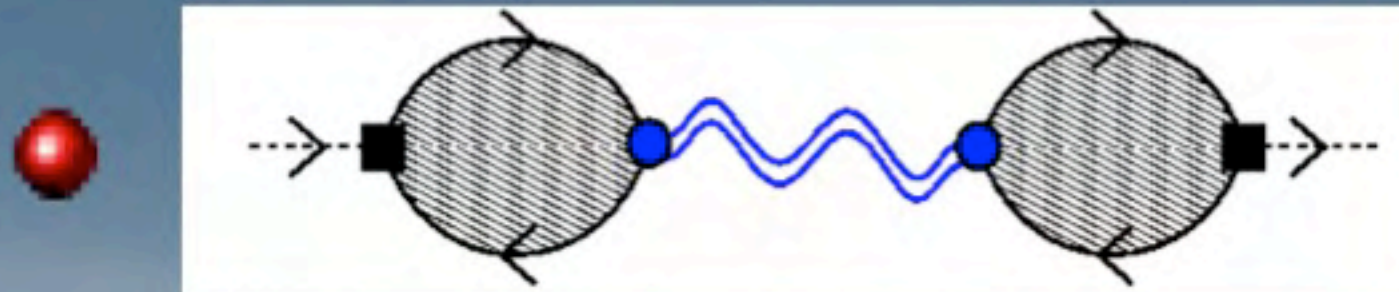
Different phonon channels in optical conductivity

gating induces z-axis asymmetry E_z

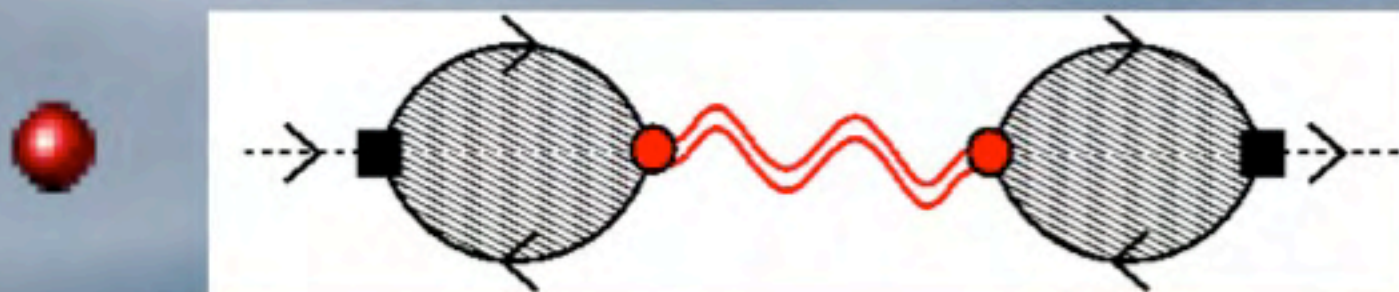
$$\Delta > 0$$

$E_g(S)$ mode also IR active!

- two main IR channels present



probes D_{AA} ph. propagator



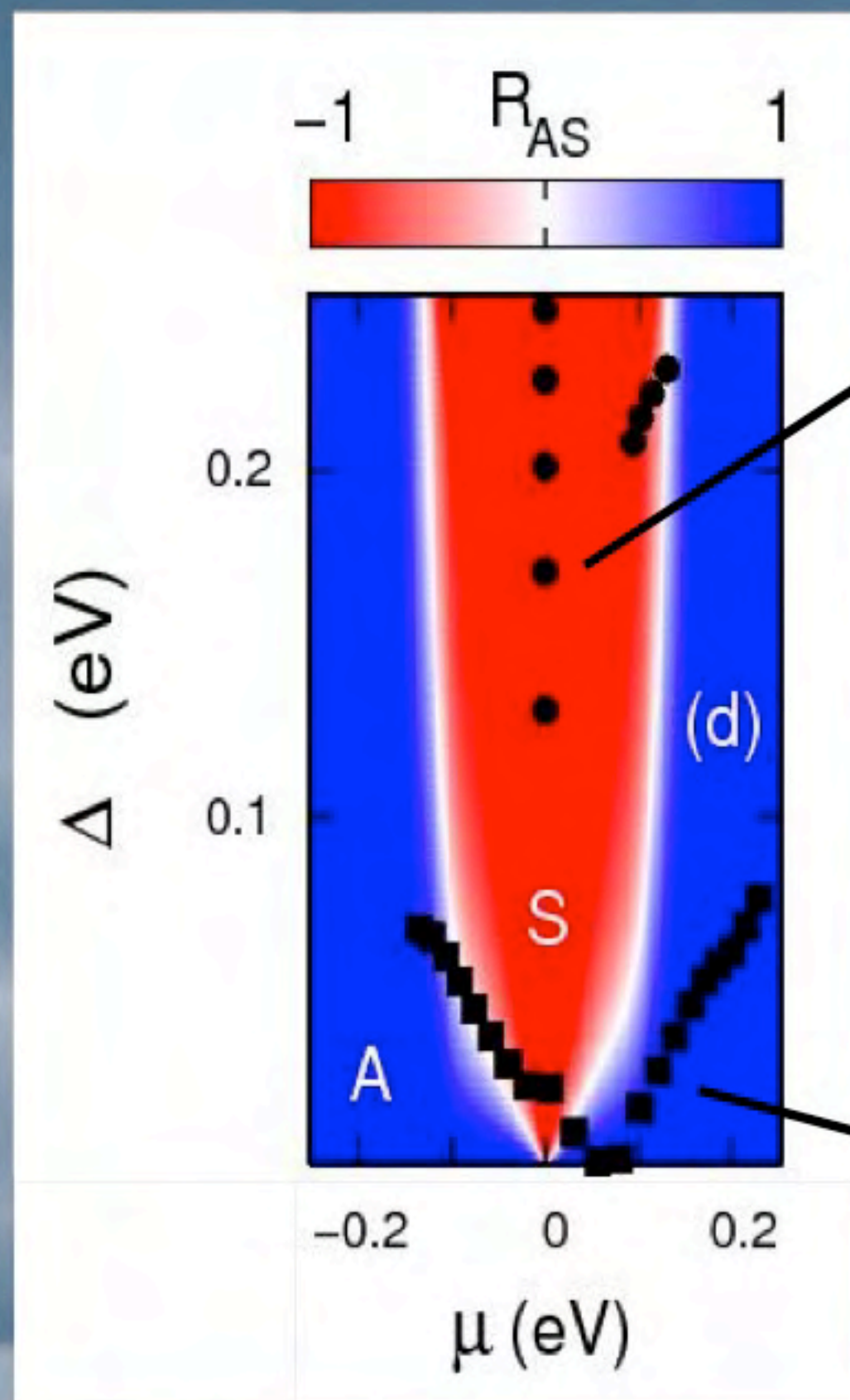
probes D_{SS} ph. propagator

relative "intensity" ruled by p_A and p_S

total spectra dependent on the relative dominance of one channel vs. the other one

Optical channels and phonon switching in optical conductivity

● Δ - μ phase diagram



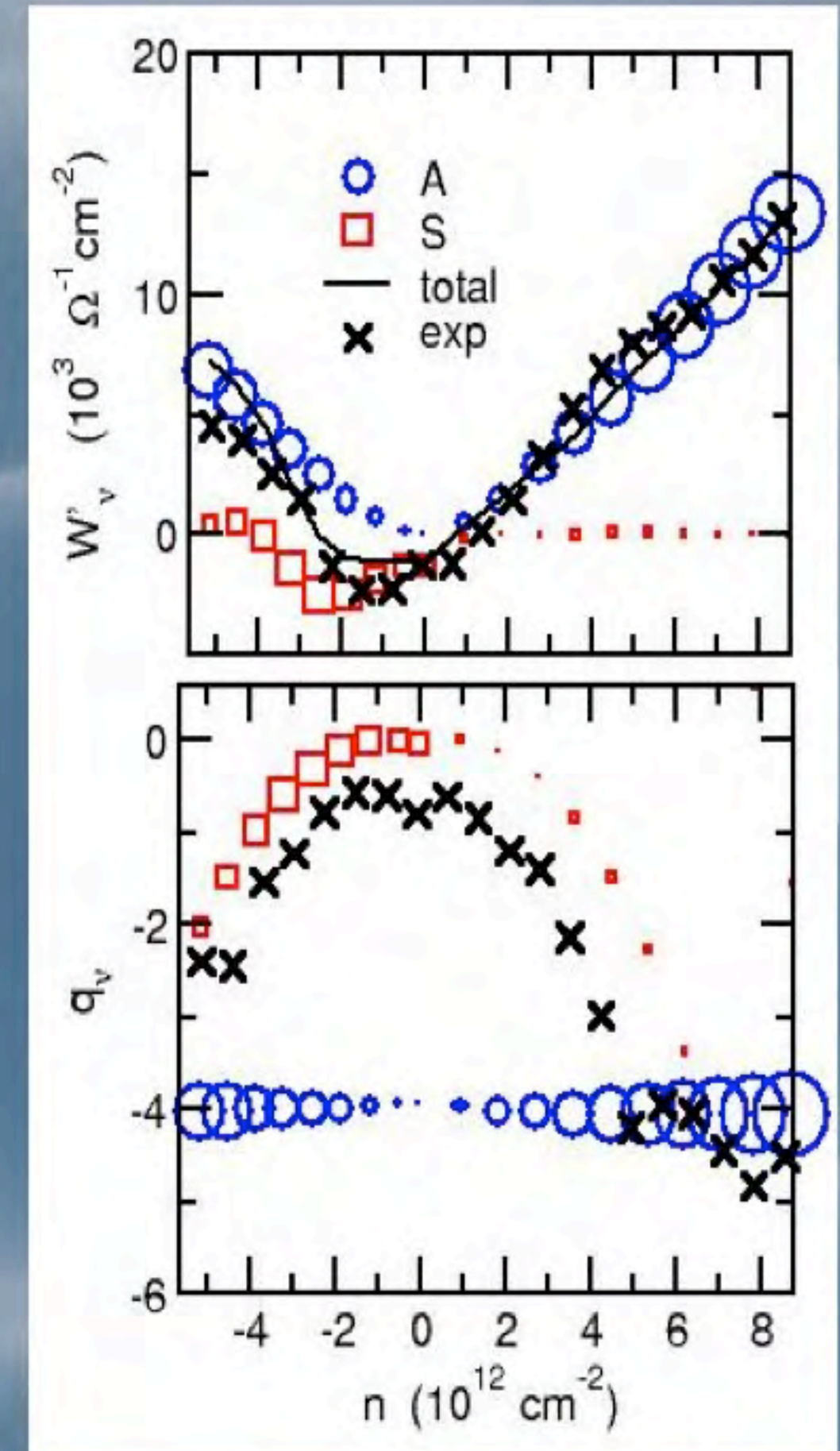
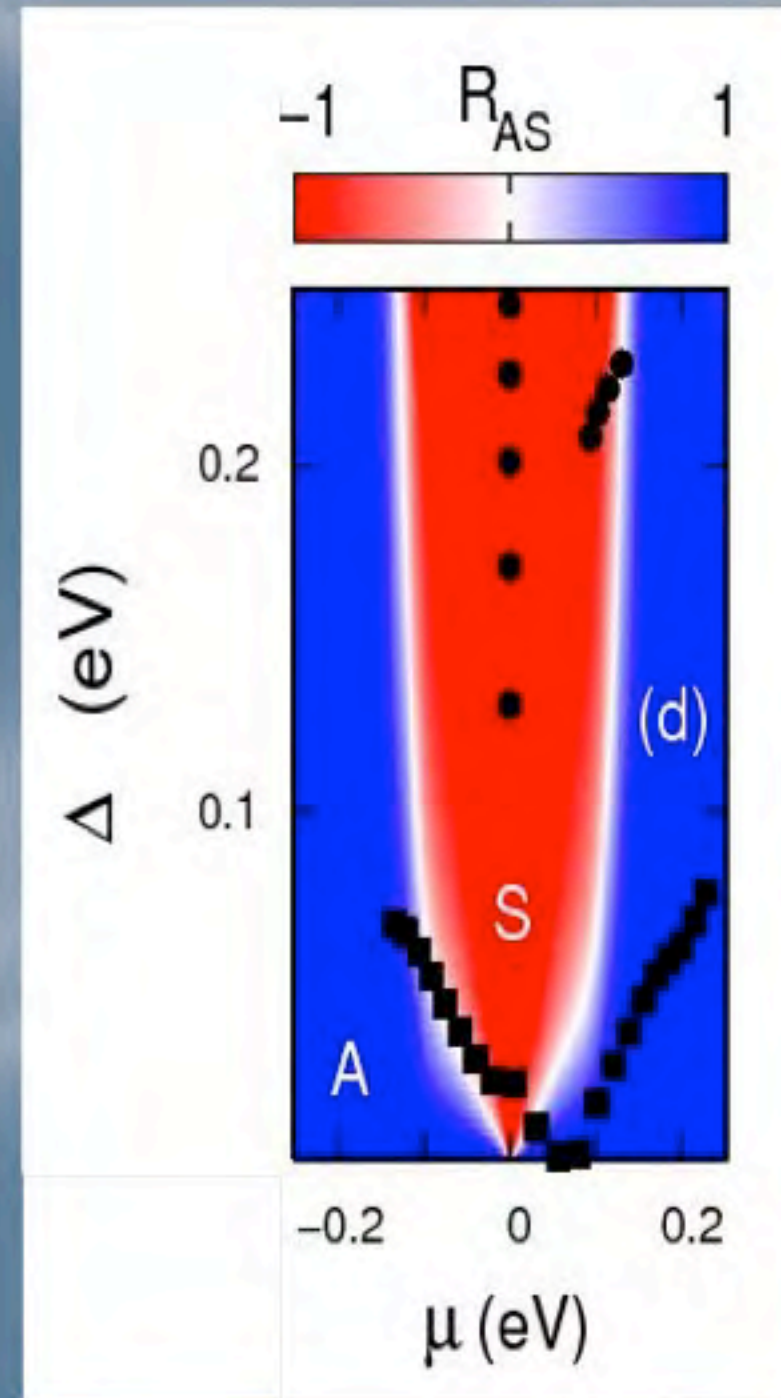
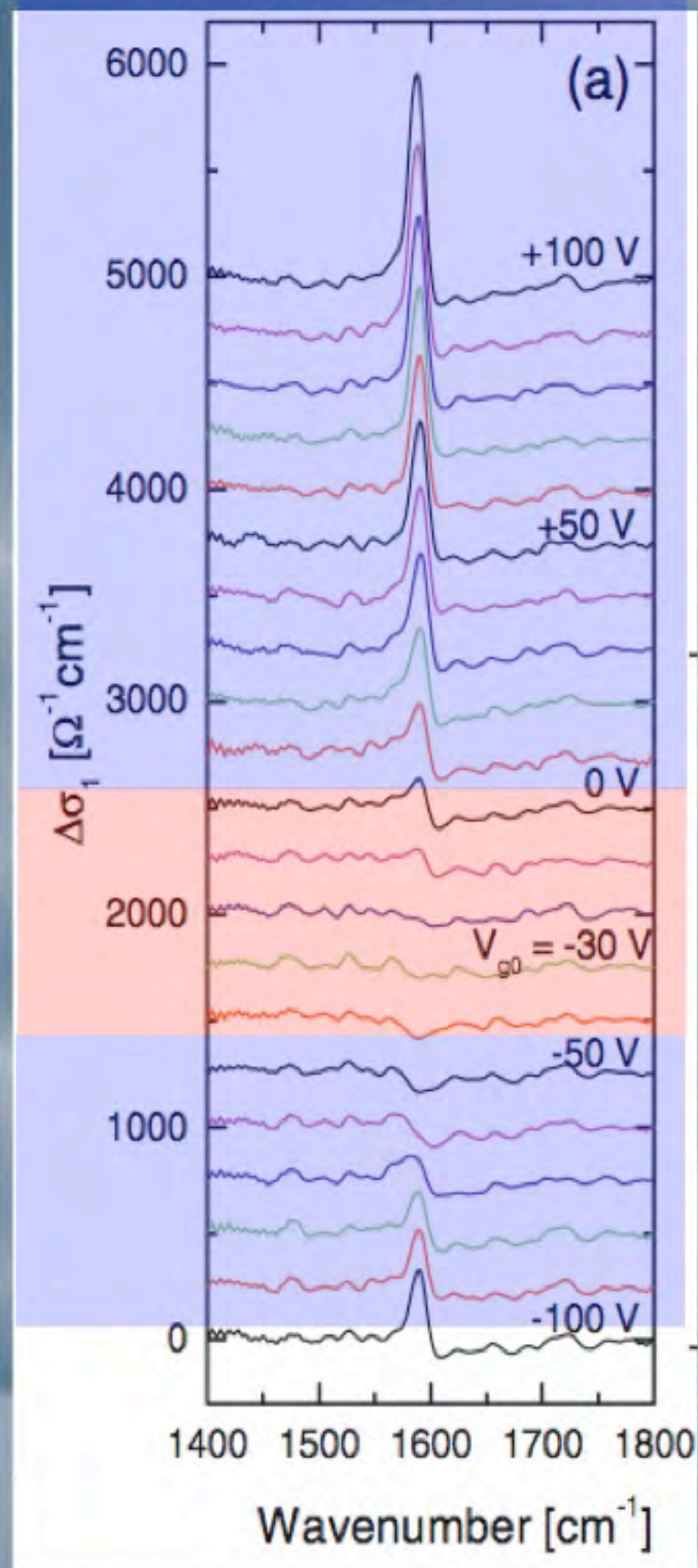
Berkeley

E_u -A and E_g -S modes
dominant in different regions
of phase diagram:
possible switching of intensity
from one mode to other one

Geneve

Es. Phonon switching in optical conductivity

Geneve group

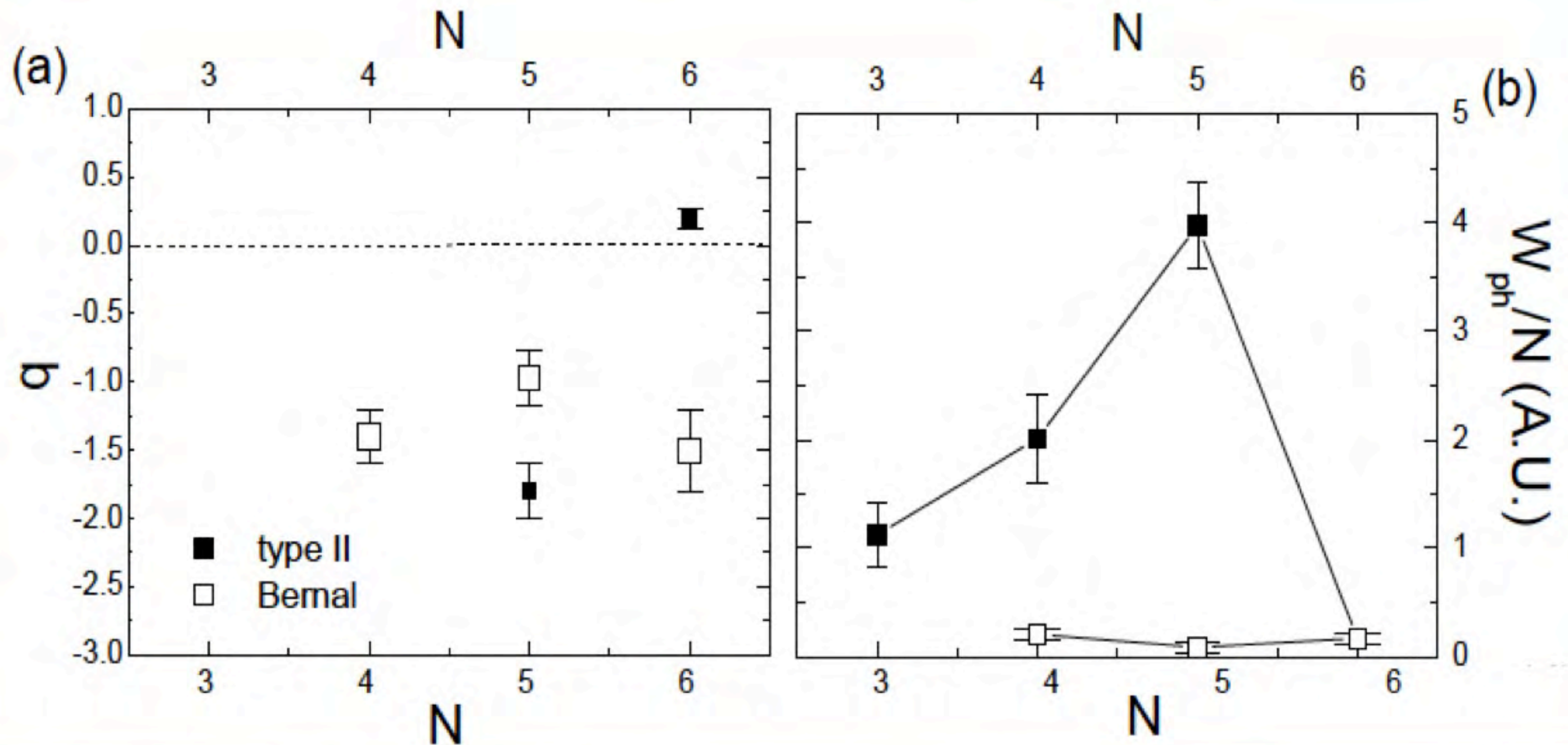


E Cappelluti et al, PRB 82, 041402 (2010)

experimental integrated area and Fano asymmetry
interpolates and switches from A to S mode

AB Kuzmenko et al, PRL 103, 116804 (2009)

Perspectives: multilayer graphene and stacking



ZQ Li et al., preprint (2011)

intensity and Fano asymmetry strong depending on N -layer and stacking order

Conclusions

- unified theory of IR intensity and Fano profile
- different phonon mode peak triggered by different channels
- complete phase diagram for charging and Fano properties
- phonon intensity switching observed in experimental data
- suitable tool to characterize graphene systems (Δ , n)

PRL 103, 116804 (2009)

PHYSICAL REVIEW LETTERS

week ending
11 SEPTEMBER 2009

Gate Tunable Infrared Phonon Anomalies in Bilayer Graphene

A. B. Kuzmenko,¹ L. Benfatto,^{2,3,4} E. Cappelluti,^{3,4} I. Crassee,¹ D. van der Marel,¹ P. Blake,⁵
K.S. Novoselov,⁵ and A. K. Geim⁵

RAPID COMMUNICATIONS

PHYSICAL REVIEW B 82, 041402(R) (2010)

Phonon switching and combined Fano-Rice effect in optical spectra of bilayer graphene

E. Cappelluti,^{1,2} L. Benfatto,^{1,2} and A. B. Kuzmenko³

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