

Deforming Single and Multilayer Graphenes in Tension and Compression



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FORTH- Graphene Centre



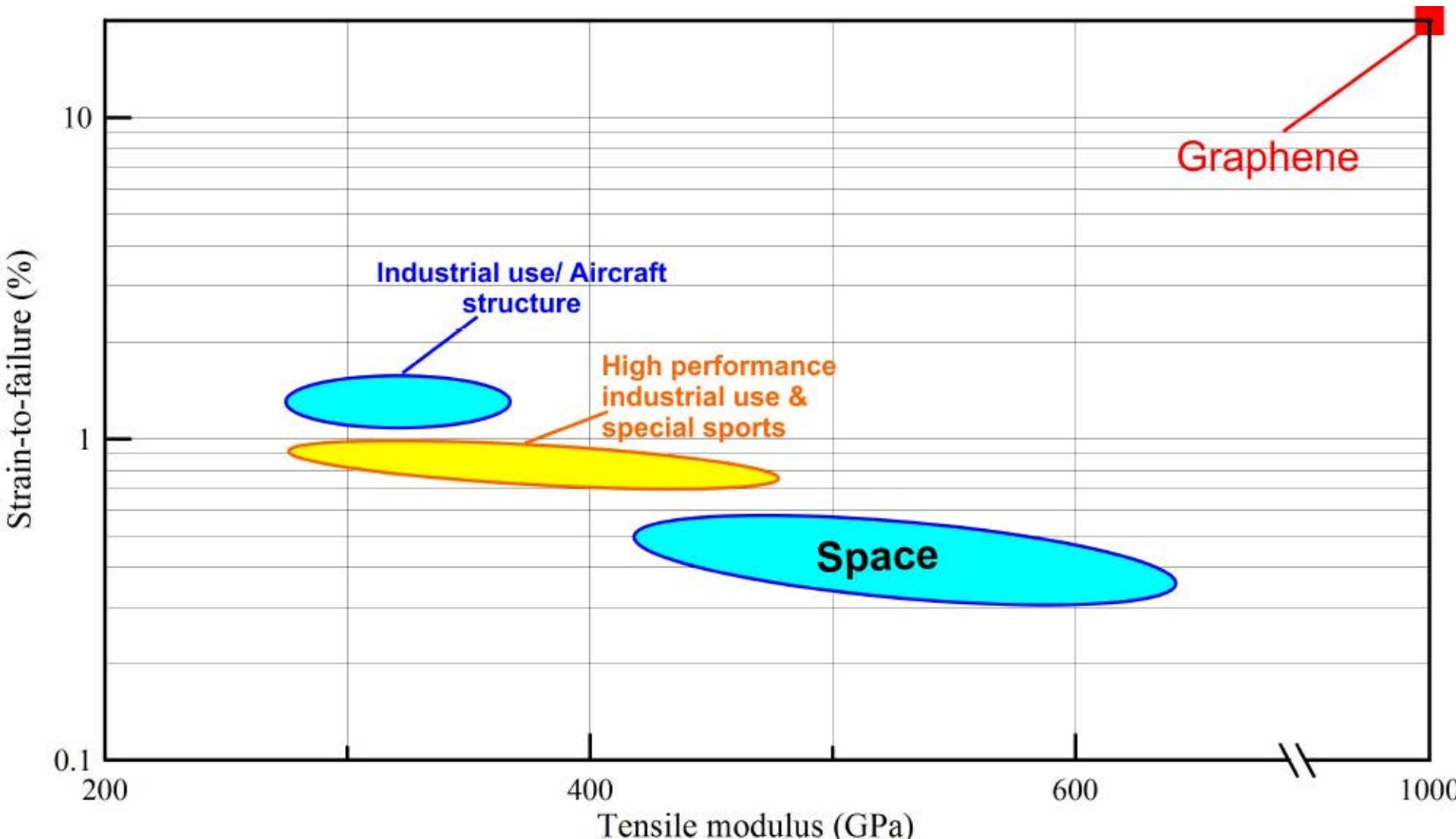
- ♦ ICP: Physics-mechanical (Patras)
- ♦ IESL: Devices (Heraklion)
- ♦ IACM: Modeling (Heraklion)



Background

Mechanical behaviour of graphene:

High stiffness, high strength, high ductility (toughness)...



Current Status/ Aims

- ❖ A great deal of modeling work (*ab initio* & other) has been accomplished (*NB. large diversity of values*).

Progress towards verification:

- ❖ Relative little experimental work (mainly bending) for freely-suspended flakes
- ❖ Axial deformation in **tension** (up to 1.5%) and **compression** (up to failure) has been accomplished on flexed beams in combination with simultaneous Raman measurements



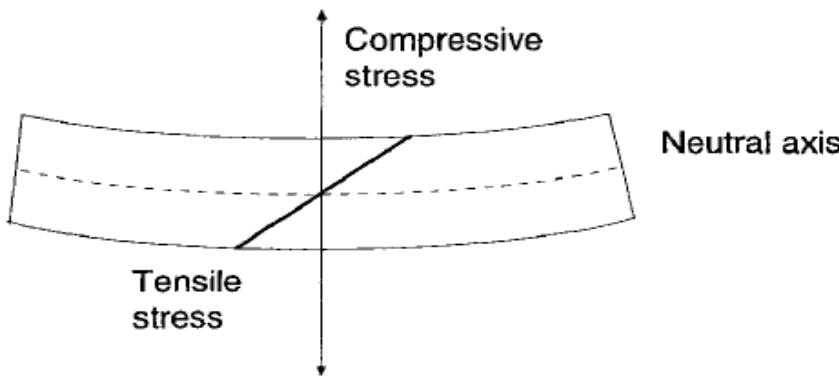
Bending Experiments



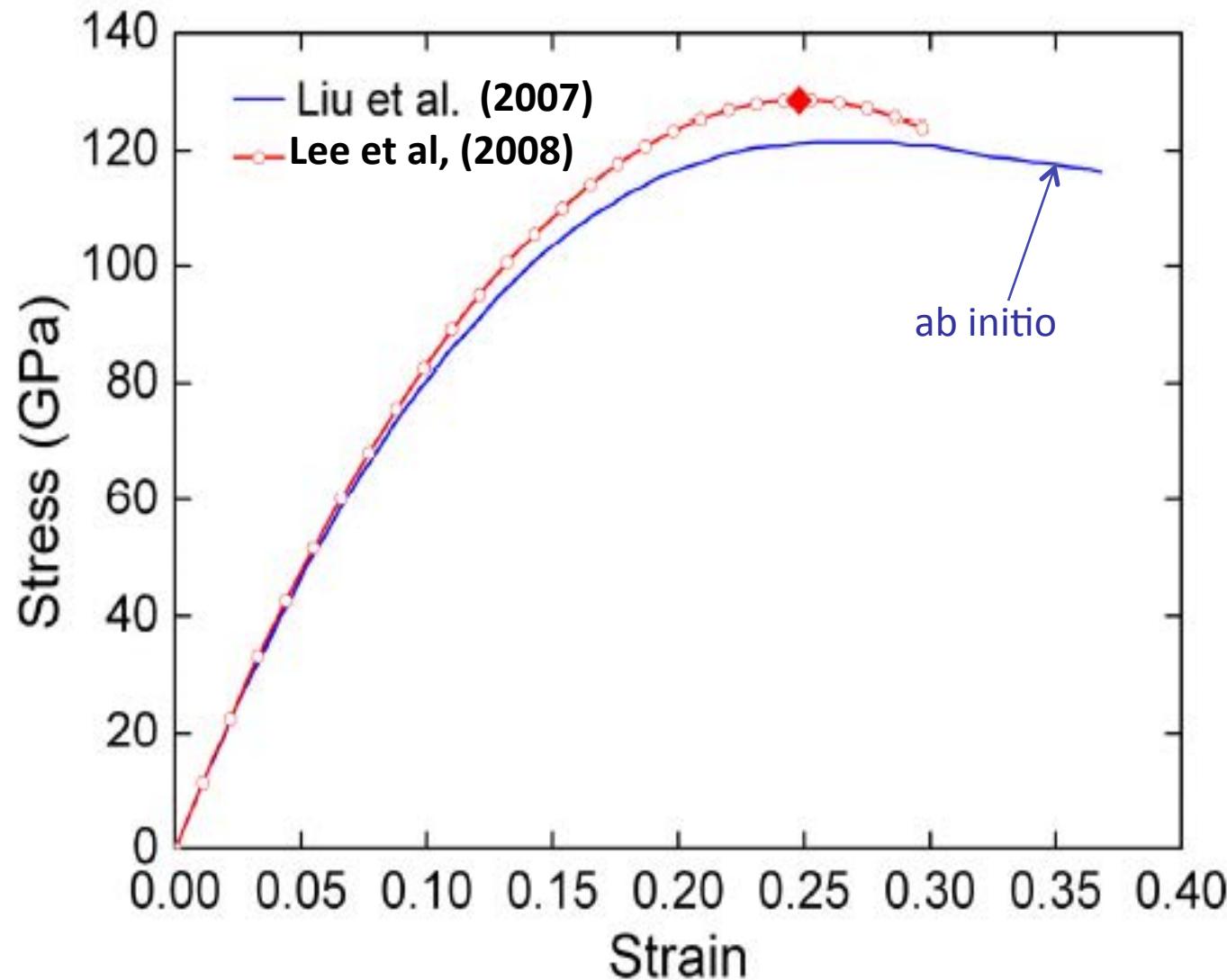
Plate vs Membrane Analysis

How should we treat graphene?

- ❖ **Membranes** exhibit zero bending stiffness (*NB. graphene exhibits a finite value of κ*). They can only sustain tensile loads; their inability to sustain compressive loads leads to wrinkling.
- ❖ **Plates** have finite thicknesses that normally give rise to internal stress/ strain distribution during bending. The deflection of the mid-plane is small compared to thickness.



Graphene as a membrane: past bending experiments



Lee et al, *Science*, 2008



Cantilever Mechanics

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DIALOGO SECONDO

fin qui dichiarate, non sarà difficile l'intender la ragione, onde au-
uenga, che un Prisma, o Cilindro solido di vetro, acciaio, legno, o
altra materia frangibile, che sospeso per lungo sosterrà gravissimo
peso, che glisia attaccato, mà in trauerso (come poco fa diceuamo) da
minor peso assai potrà tal volta essere spezzato, secondo che la sua
lunghezza eccederà la sua grossezza. Imperò che figuriamoci il Pris-
ma solido AB, CD fitto in un muro dalla parte AB, e nell'altra
estremità s'intenda la forza del Peso E, (intendendo sempre il mu-
ro effer eretto all'Orizonte, & il Prisma, o Cilindro fitto nel muro
ad angoli retti) è manifesto che donendosi spezzare si romperà nel
luogo B, dove
il taglio del

Galilei, Galileo (1564-1642)
Discorsi e dimostrazioni
matematiche, intorno à due
nuove scienze.

rements)



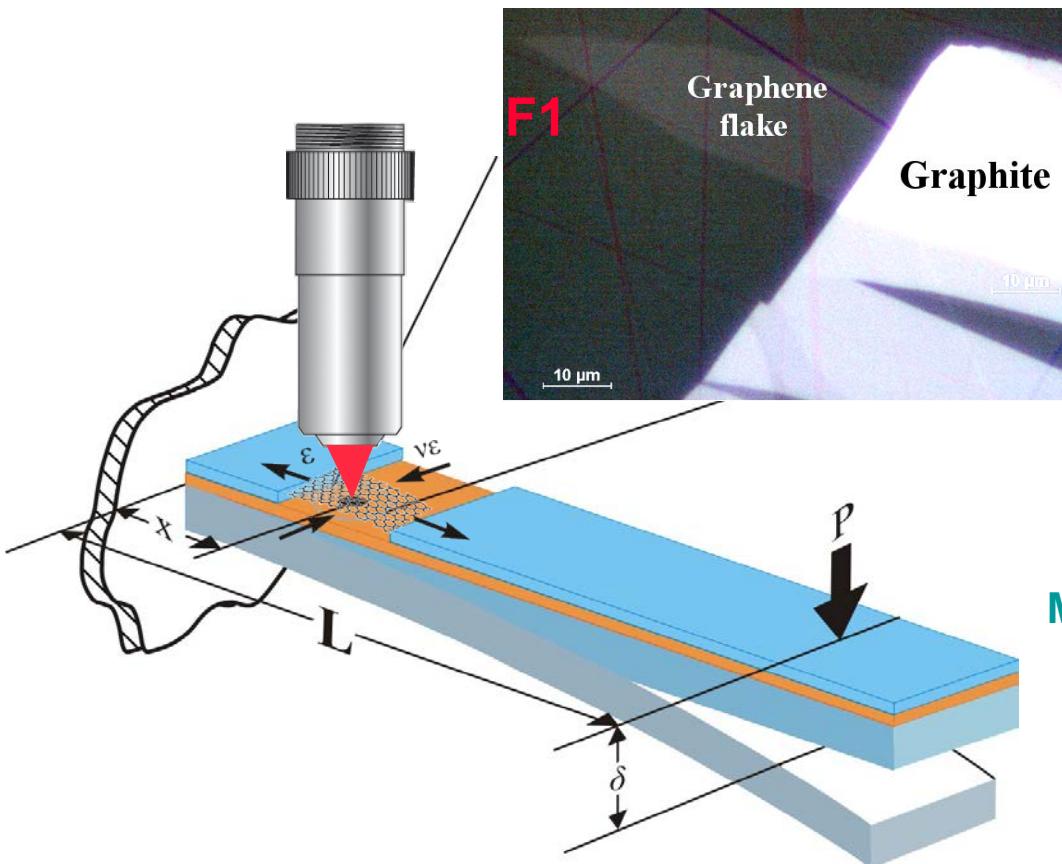
aei jouao B A
e l'altra parte
della Leua,
nella quale è
posta la resi-
stenza, che
consiste nel-
lo staccamen-
to, che s'hà
da fare della
parte del soli-
do B D, che è

fuor del muro, da quella che è dentro; e per le cose dichiarate il mo-
mento della forza posta in C al momento della resistenza che stà
nella

(tension & compre-



Experimental set-up for application of uniaxial strain

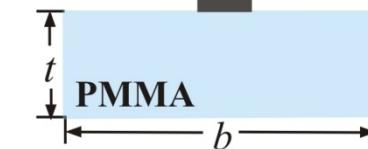


Materials & Geometry

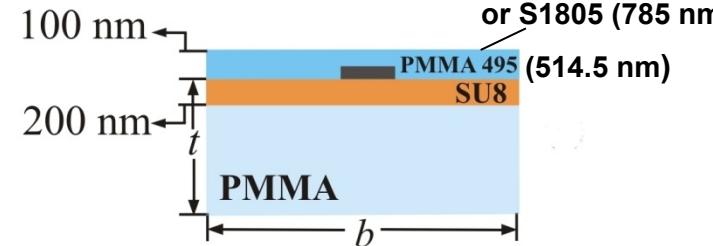
- SU8 photo resist epoxy-based polymer
- PMMA beam substrate ($2.9 \times 12.0 \times 70$) mm³
- $x = 10.4$ mm and $L = 70$ mm

Simply-supported flake

Graphene flake



Embedded flake



Mechanical strain at the top of the beam

$$\varepsilon(x) = \frac{3t\delta}{2L^2} \left(1 - \frac{x}{L}\right)$$

δ : deflection of the beam neutral axis

L : span of the beam

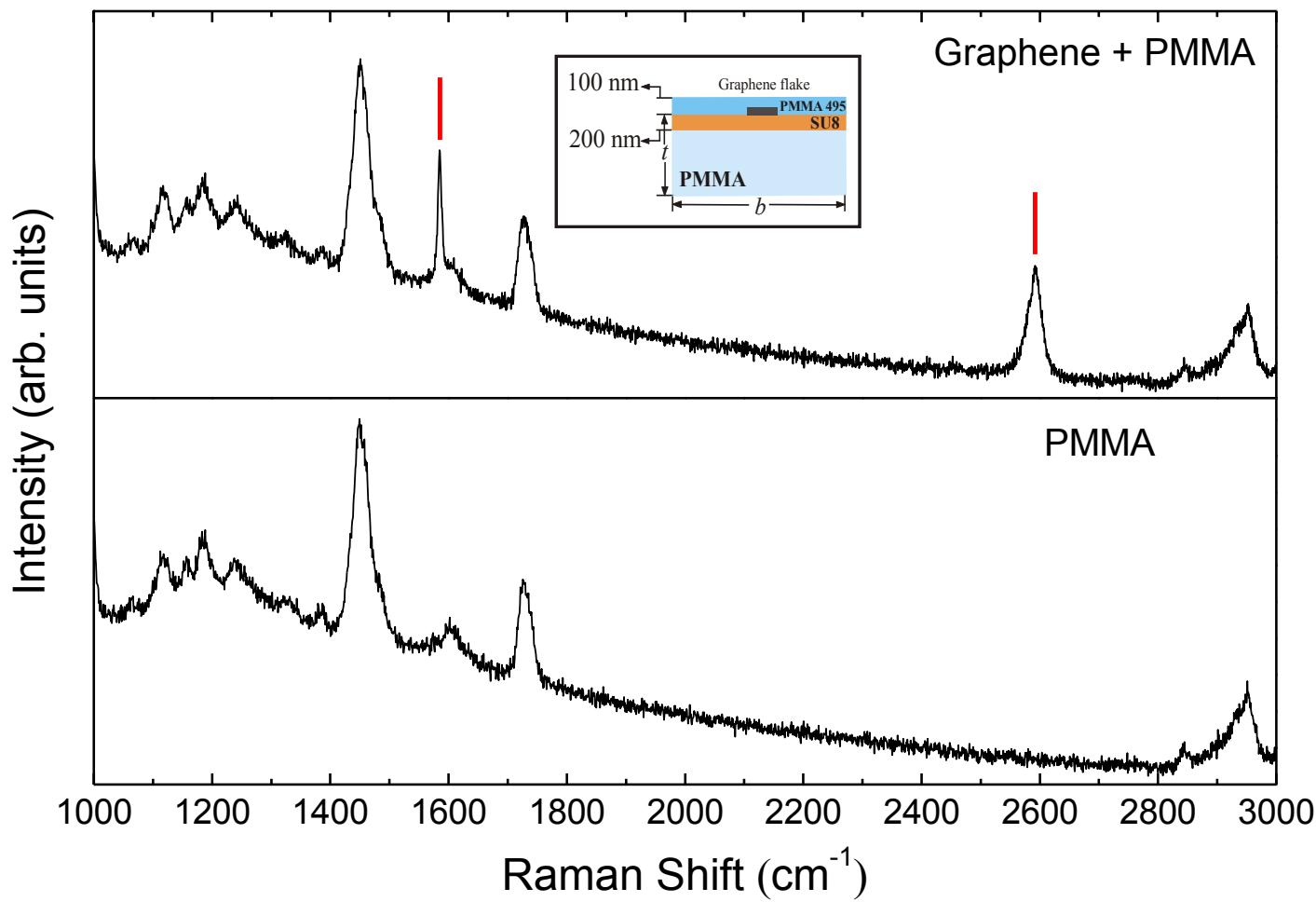
t : beam thickness

Operating limits:

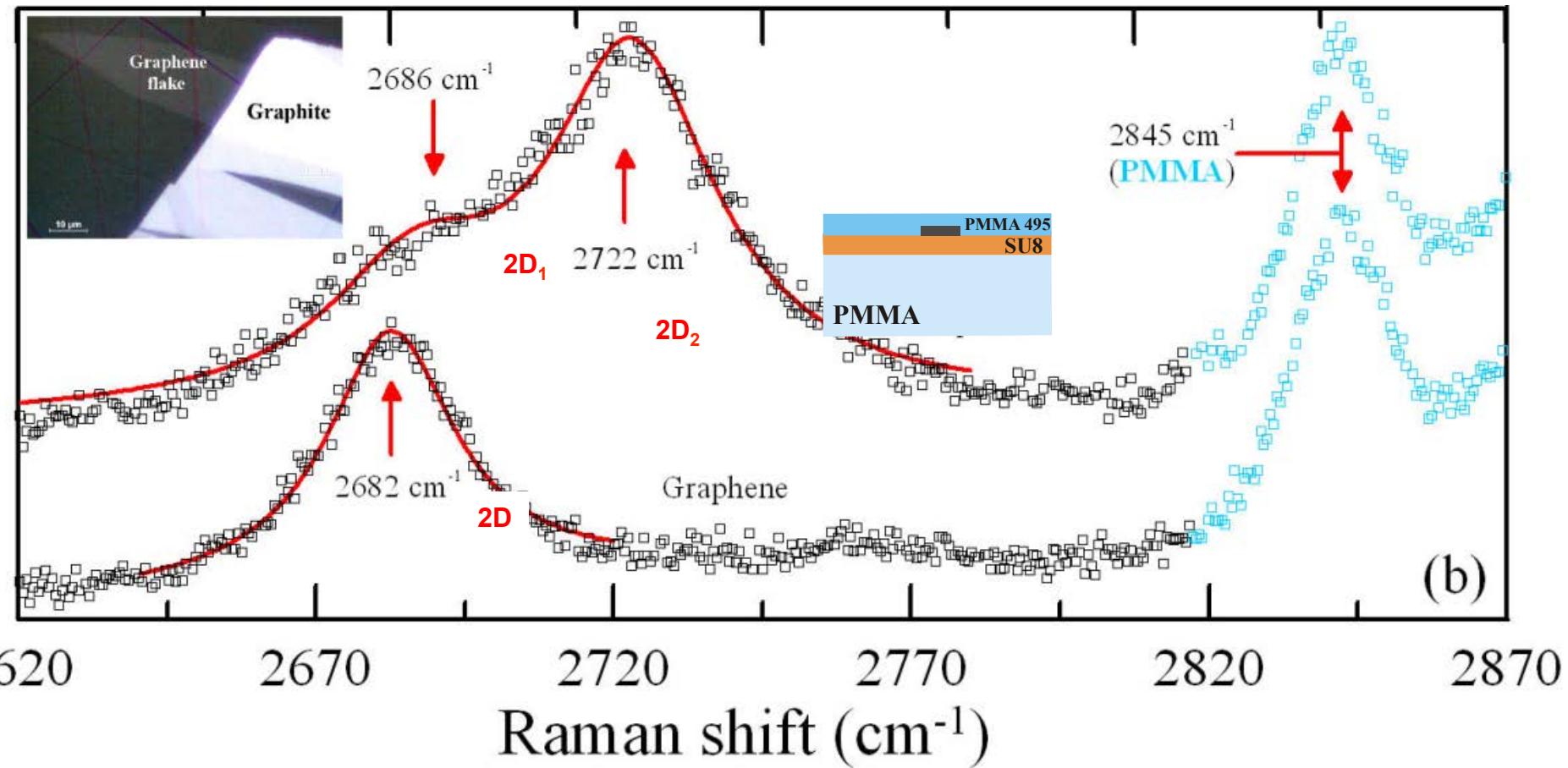
- $L \gg 10\delta_{\max}$
- $-1.5\% < \varepsilon < 1.5\%$



Raman Spectra of embedded layer graphene inside PMMA



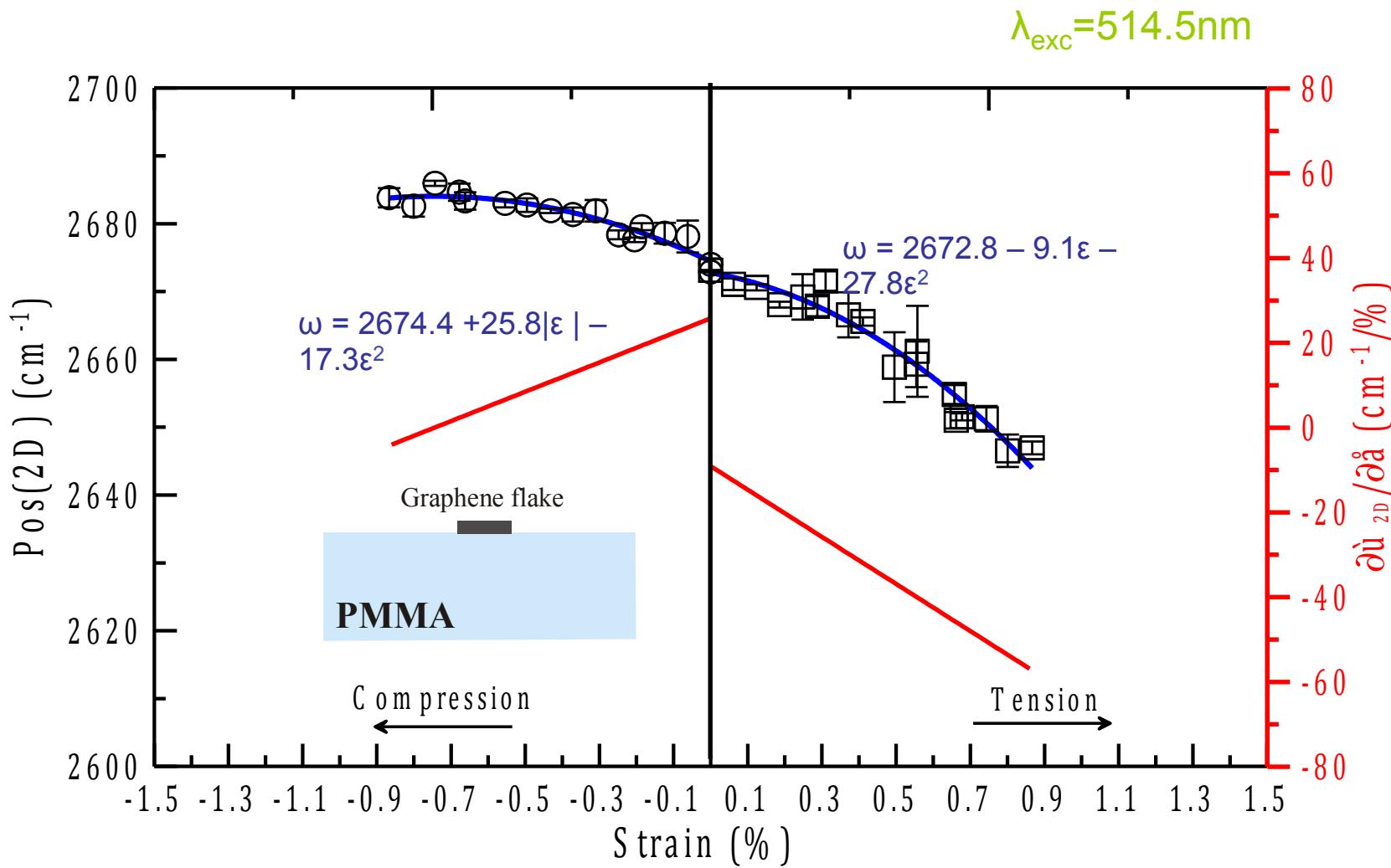
Raman spectra of 2D-peak from embedded graphene flakes and bulk graphite



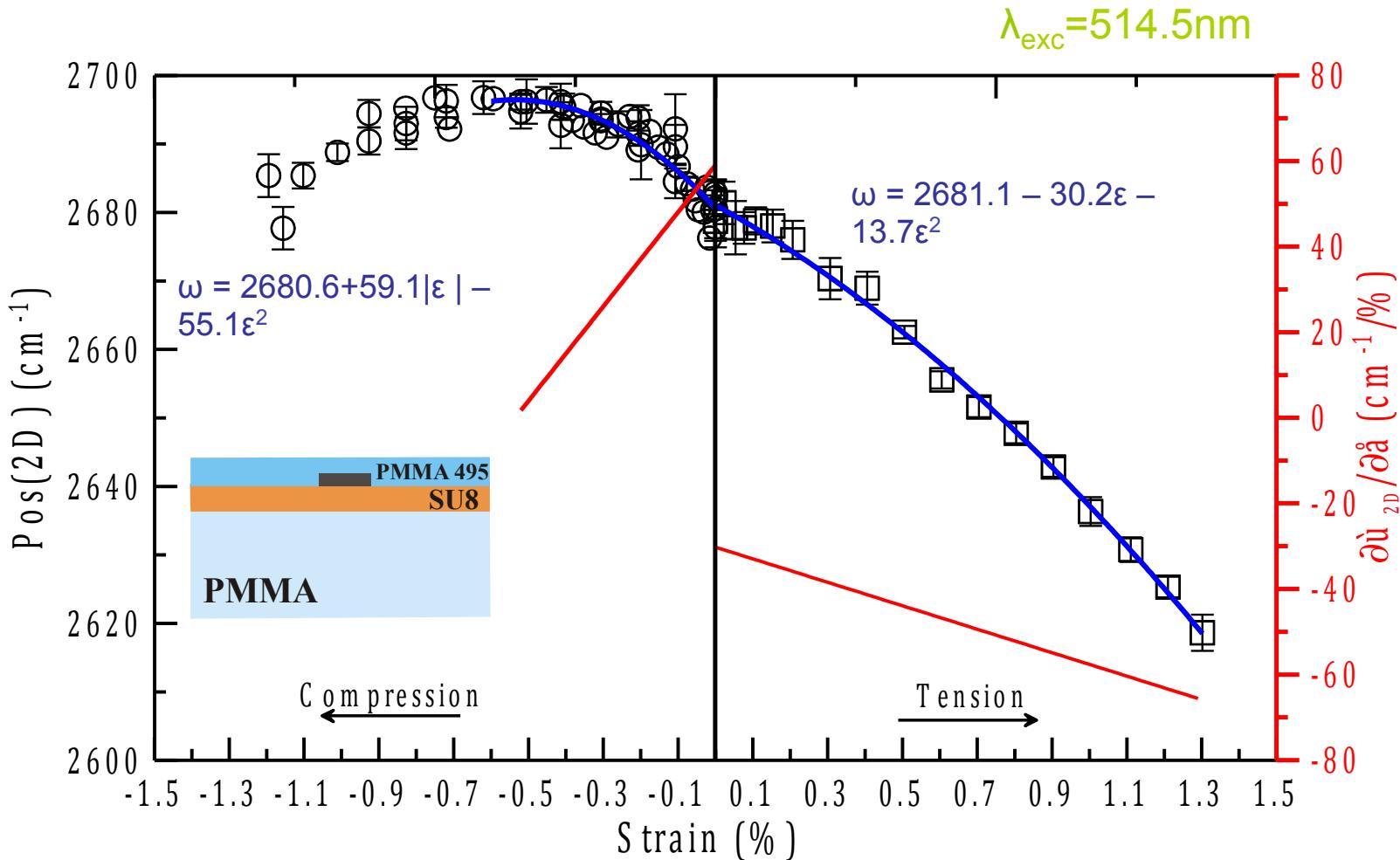
Tsoukleri et al. *Small* 2009, 5, 2397]



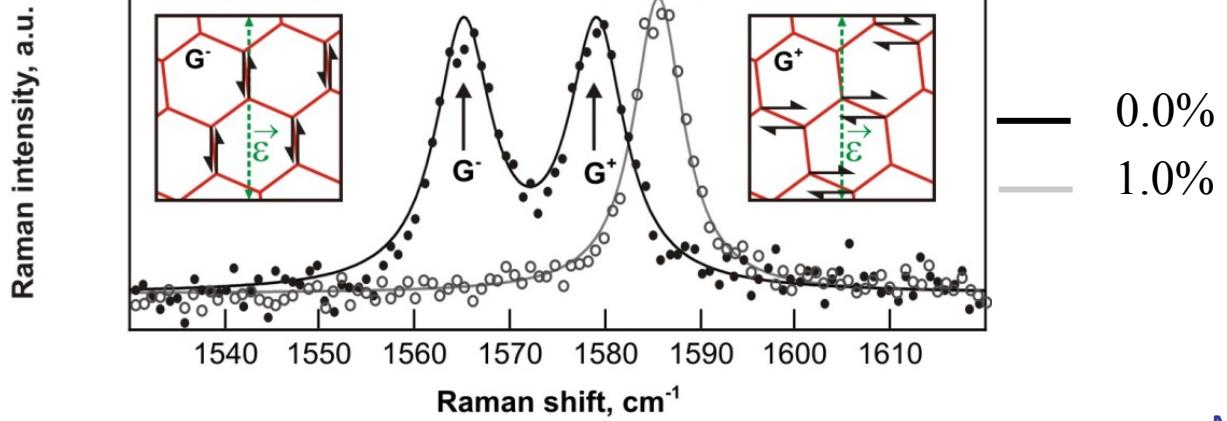
Simply-supported (“bare”) flake



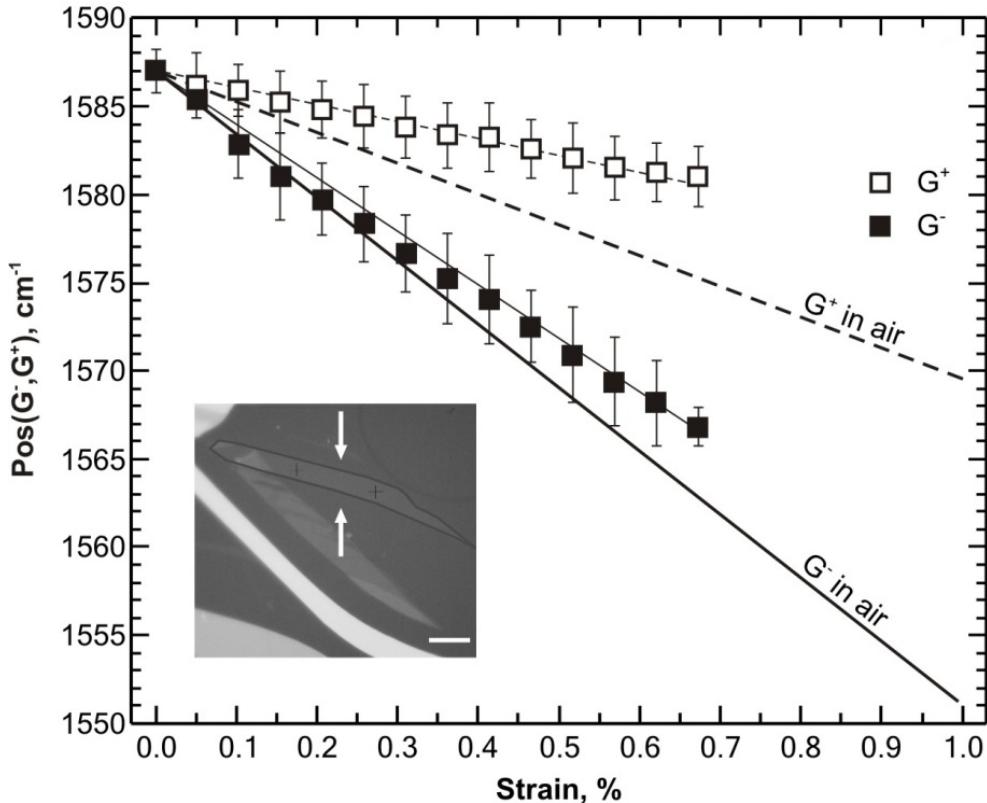
Fully embedded flake



G peak vs. strain (no residual strain)



Mohiudin et al, *PRB*, 2009
Frank et al, *ACS-Nano*, 2010

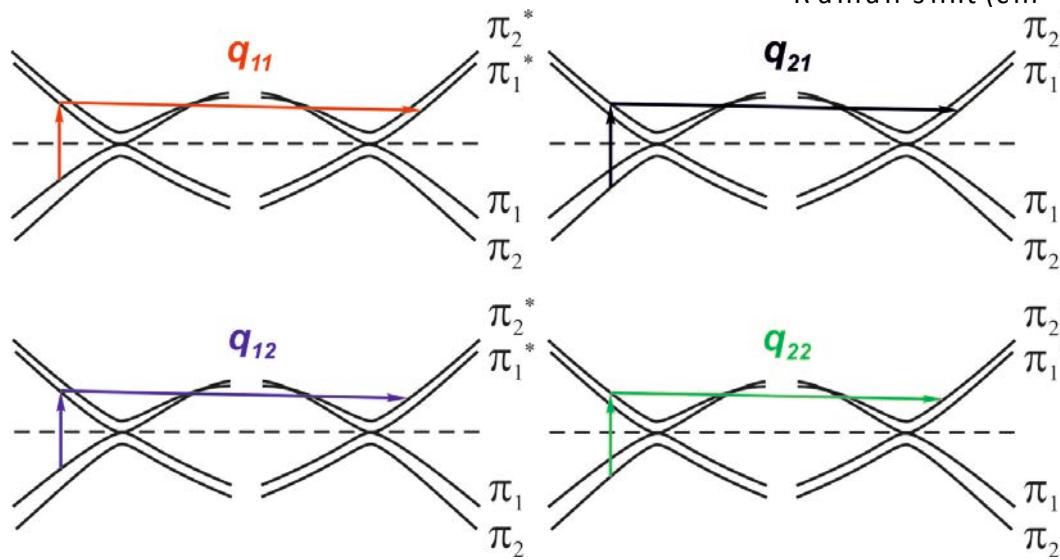
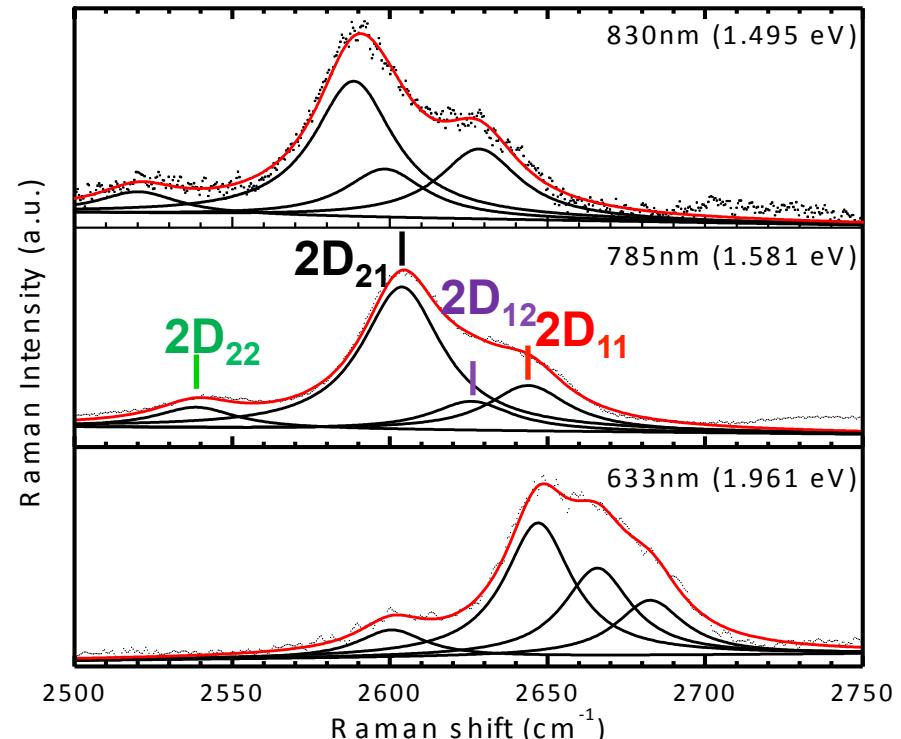
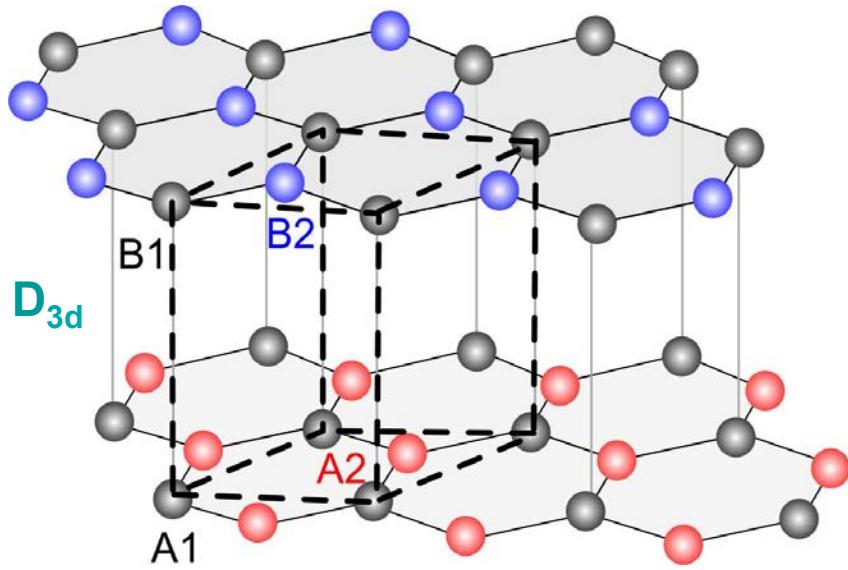


$$\partial \omega_{G^-} / \partial \epsilon = -36.0 \text{ cm}^{-1}/\%$$

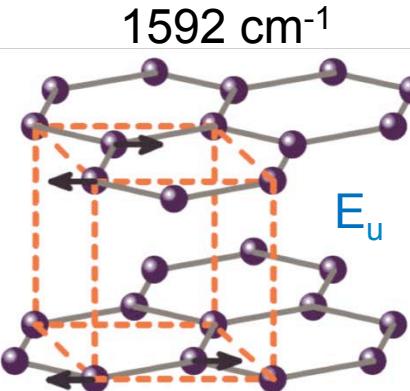
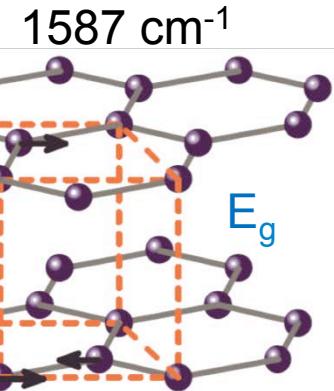
$$\partial \omega_{G^+} / \partial \epsilon = -17.5 \text{ cm}^{-1}/\%$$



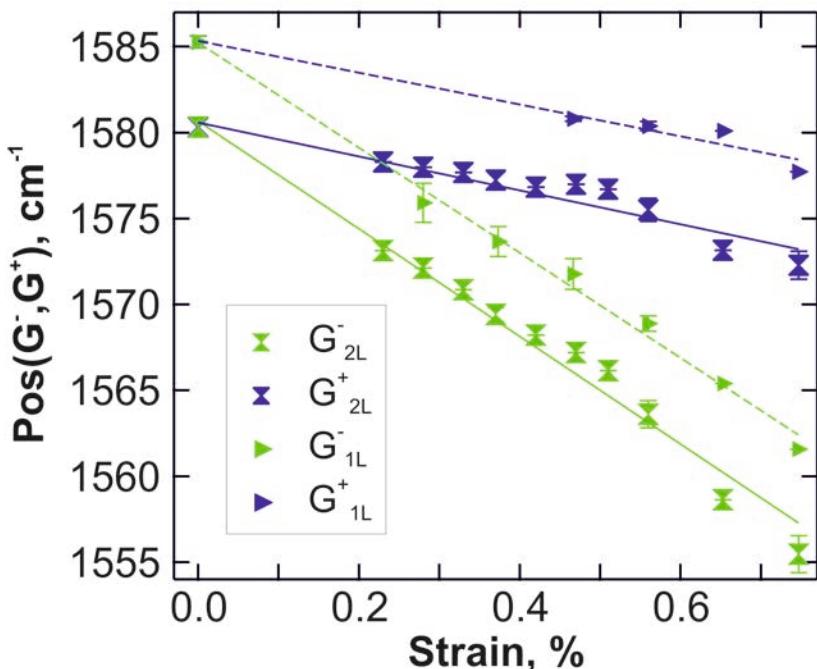
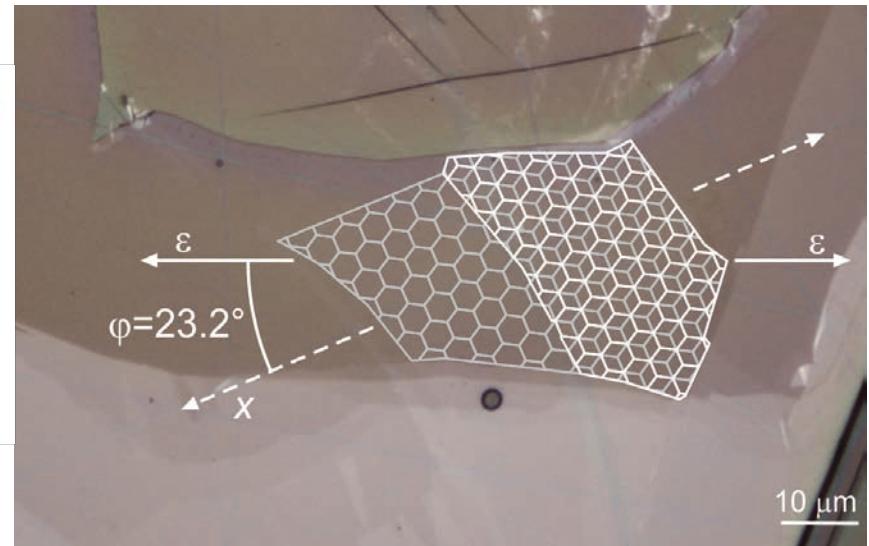
Loading a graphene bilayer



Graphene bilayer under uniaxial tension – G peak



[Yan et al. PRB 77, 125401 (2009)]



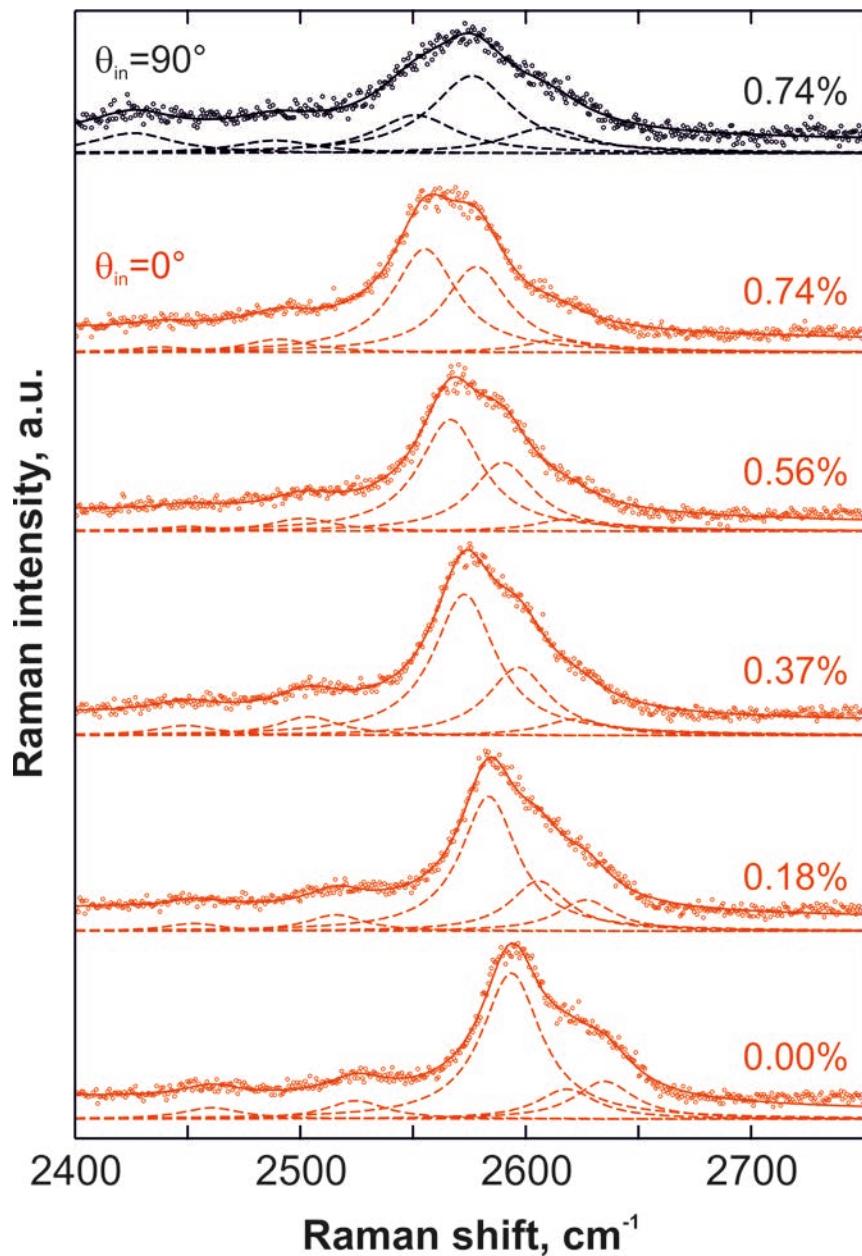
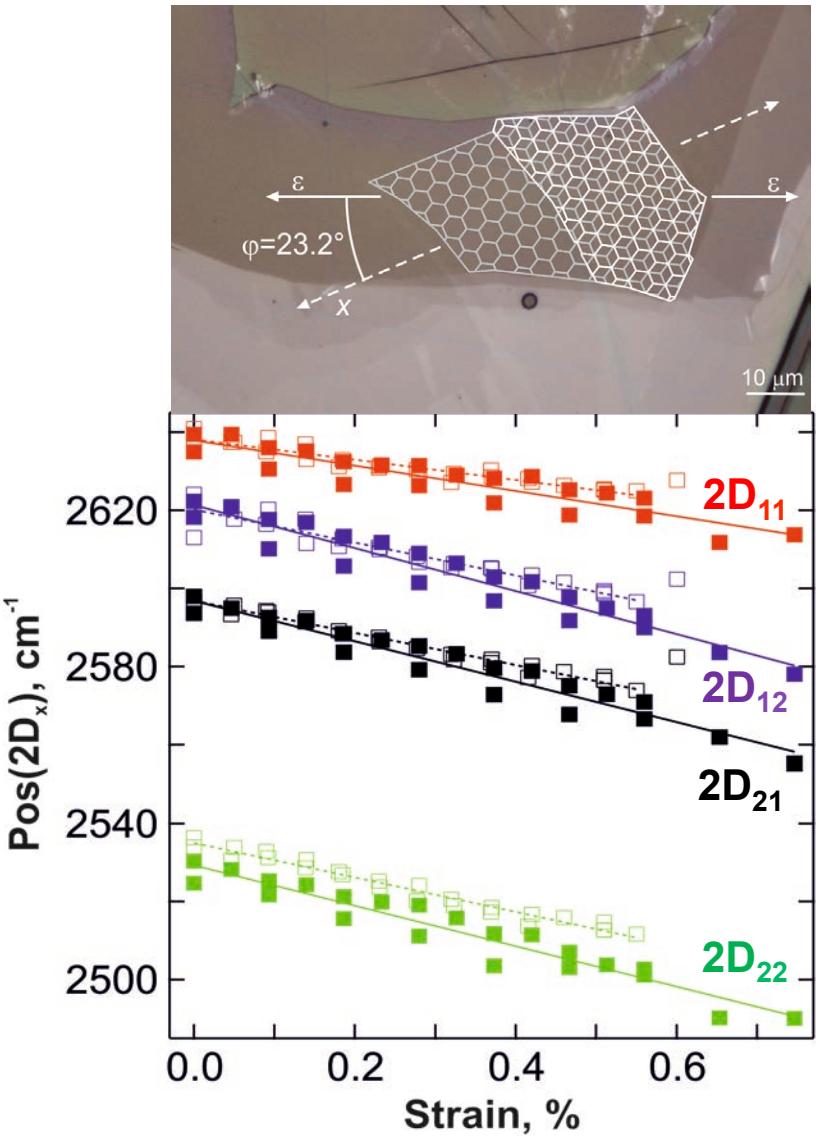
$$\partial \omega_G^+(2L) / \partial \varepsilon = -9.9 \pm 4.9 \text{ cm}^{-1} / \%$$

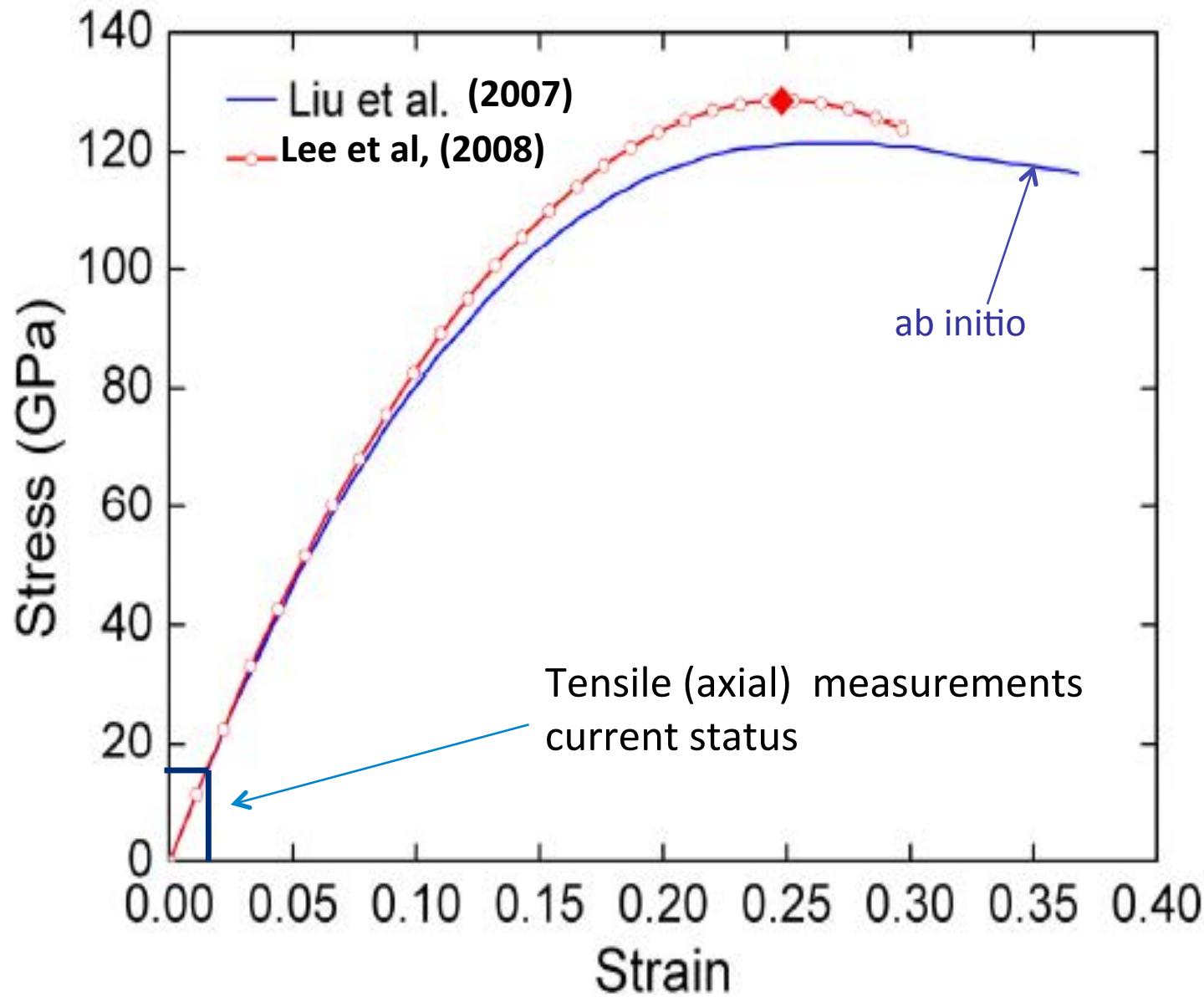
$$\partial \omega_G^-(2L) / \partial \varepsilon = -31.3 \pm 5.4 \text{ cm}^{-1} / \%$$

Frank et al, to be submitted, 2011



Graphene bilayer under uniaxial tension – 2D peak



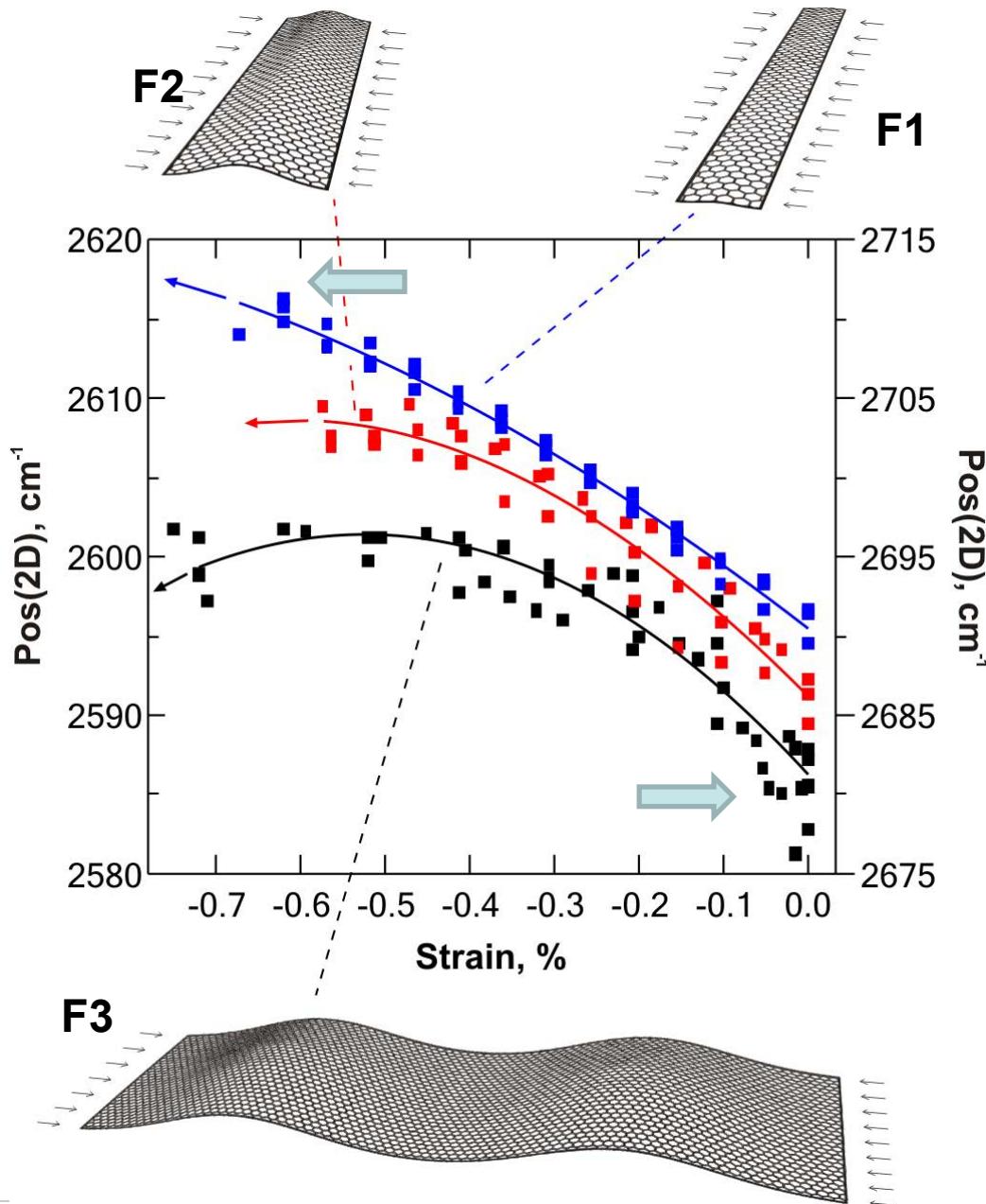


Compression

(Measurements & Analysis)



Compression of embedded graphene flakes - 2D band



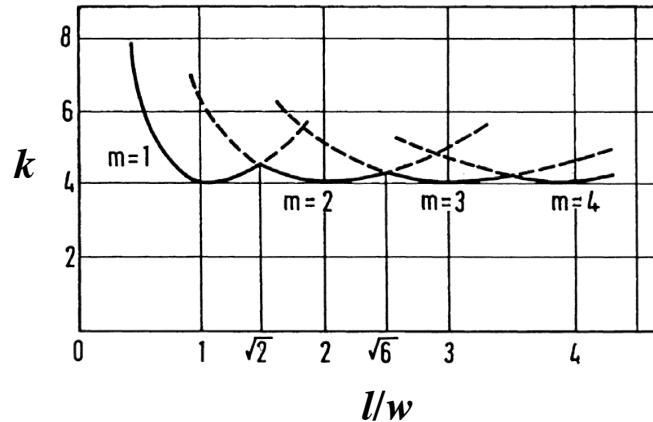
Graphene as a thin plate: critical buckling strain (1/2)

The **critical strain**, ε_c , for the buckling of a rectangular thin plate under uniaxial compression is given by the classical **Euler formula**:

$$\varepsilon_c = \frac{\pi^2 k}{w^2} \left(\frac{K}{C} \right)$$

- l : length (dimension parallel to strain)
- w : width
- m : number of half-waves to appear at the critical load
- κ : flexural rigidity, $3.18 \text{ GPa nm}^3 = 20 \text{ eV}^1$
- C : tension rigidity, 340 GPa nm^1

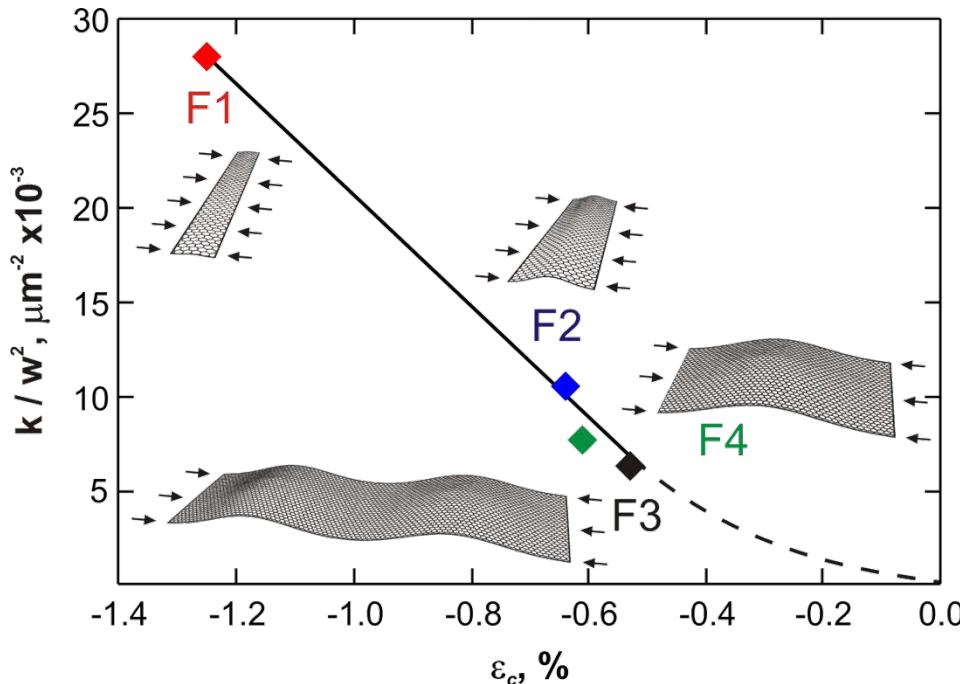
$$k = \left(\frac{mw}{l} + \frac{l}{mw} \right)^2$$



For a layer of atomic thickness in air, $\varepsilon_c \approx 10^{-9}$ (1 nanostrain)



Graphene as a thin plate: critical buckling strain (2/2)



$$\frac{k}{w^2} = a\varepsilon_c + b$$

slope

$$a = -0.03 \mu\text{m}^{-2}$$

Euler regime applies for $k > 0.05 \mu\text{m}^{-2}$

– For freely suspended flake in air:

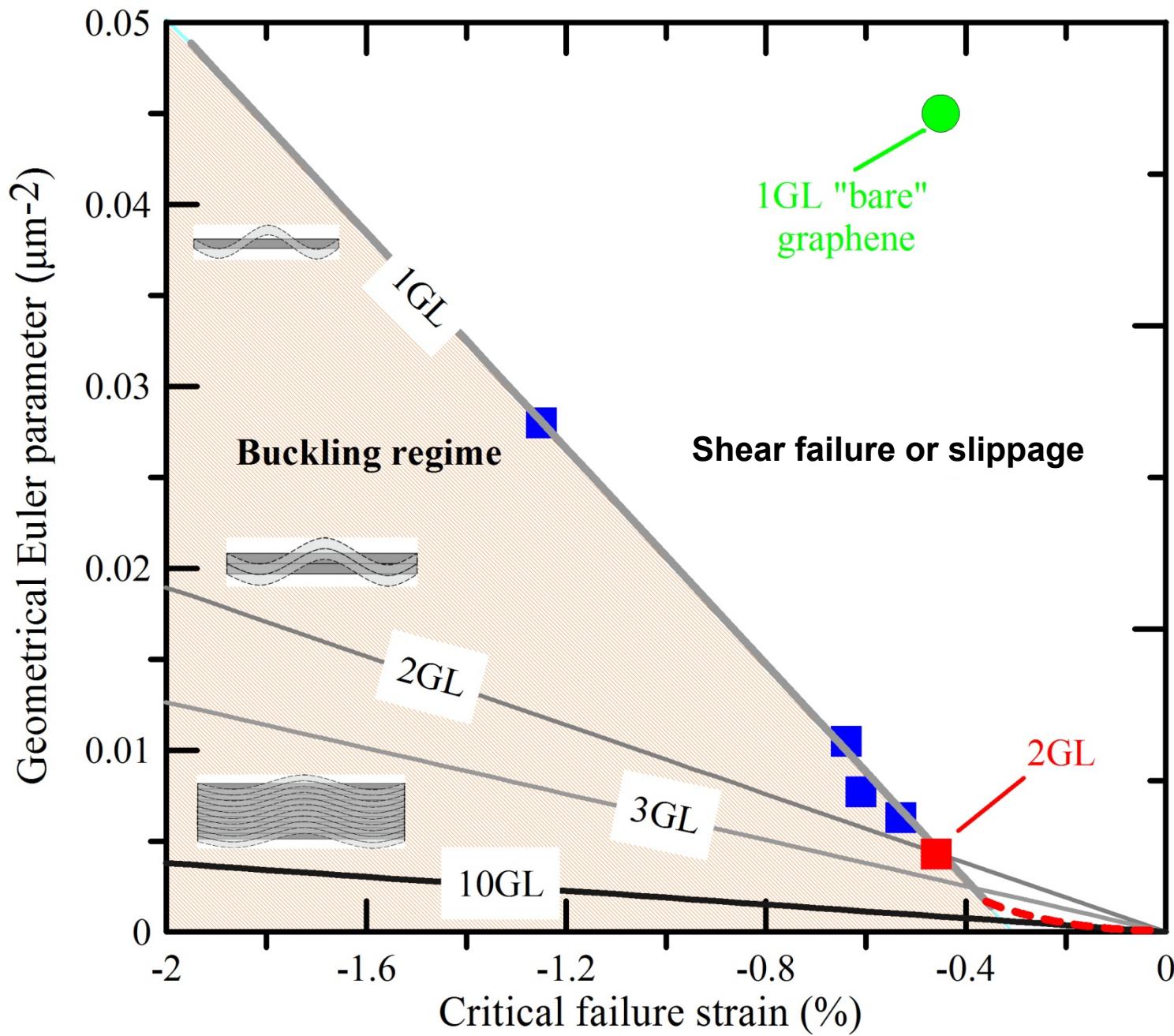
$$K = 3.18 \text{ GPa nm}^3 \sim 20 \text{ eV}$$

– For embedded flake:

$$\varepsilon_c^{embedded} = \frac{k}{w^2} \frac{K_{embedded} \pi^2}{C},$$

$$K_{embedded} = 1.2 \times 10^7 \text{ GPa nm}^3 \sim 70 \text{ MeV}$$





Bending Stiffness, κ , for $h=0.335$ nm

Specimen	κ (eV)	κ (Joules)
<i>Free-standing</i>	$\sim 20^1$	$\sim 3 * 10^{-18}$
<i>Embedded</i>	$\sim 7 * 10^7$ $(70 \text{ MeV})^2$	$\sim 1 * 10^{-11}$ (10 pJ)
<i>Simply-supported</i>	$\sim 2 * 10^7$ $(20 \text{ MeV})^2$	$\sim 3 * 10^{-12}$ $(3 \text{ pJ})^3$

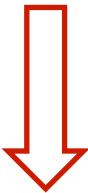
¹ Lee et al, *Science*, 2008

² Frank et al, *ACS Nano*, 2010

³ Unpublished Data



Estimation of compression strength



SLG Flake	ε_c (%) ¹	σ_c (GPa) ²	l (μm)	w (μm)	k	k / w^2 (μm^{-2})
F1	-1.25	12.5	6	56	89.12	0.028
F2	-0.64	6.4	11	50	22.71	0.011
F3	-0.53	5.3	56	25	4.02	0.006
F4	-0.61	6.1	28	23	4.14	0.008

¹ ε_c determined from the 2nd order polynomials as maxima

² Assuming a modulus of 1 TPa and a linear relationship

Typical compression strength of carbon fibres (microscale): 2-3 GPa



Stress transfer phenomena in polymer/ graphene composites



Graphene: A powerful stress/ strain sensor

Phonon stress or strain sensitivities:

G peak

$$\left(\frac{\partial \bar{G}}{\partial \sigma} \right)_T \sim -2.7 \text{ (cm}^{-1}\text{GPa}^{-1}\text{)}$$

$$\left(\frac{\partial \bar{G}}{\partial \varepsilon} \right)_T \sim -2700 \text{ cm}^{-1}$$

2D peak

$$\left(\frac{\partial (2D)}{\partial \sigma} \right)_T \sim -6.0 \text{ (cm}^{-1}\text{GPa}^{-1}\text{)}$$

$$\left(\frac{\partial (2D)}{\partial \varepsilon} \right)_T \sim -6000 \text{ cm}^{-1}$$

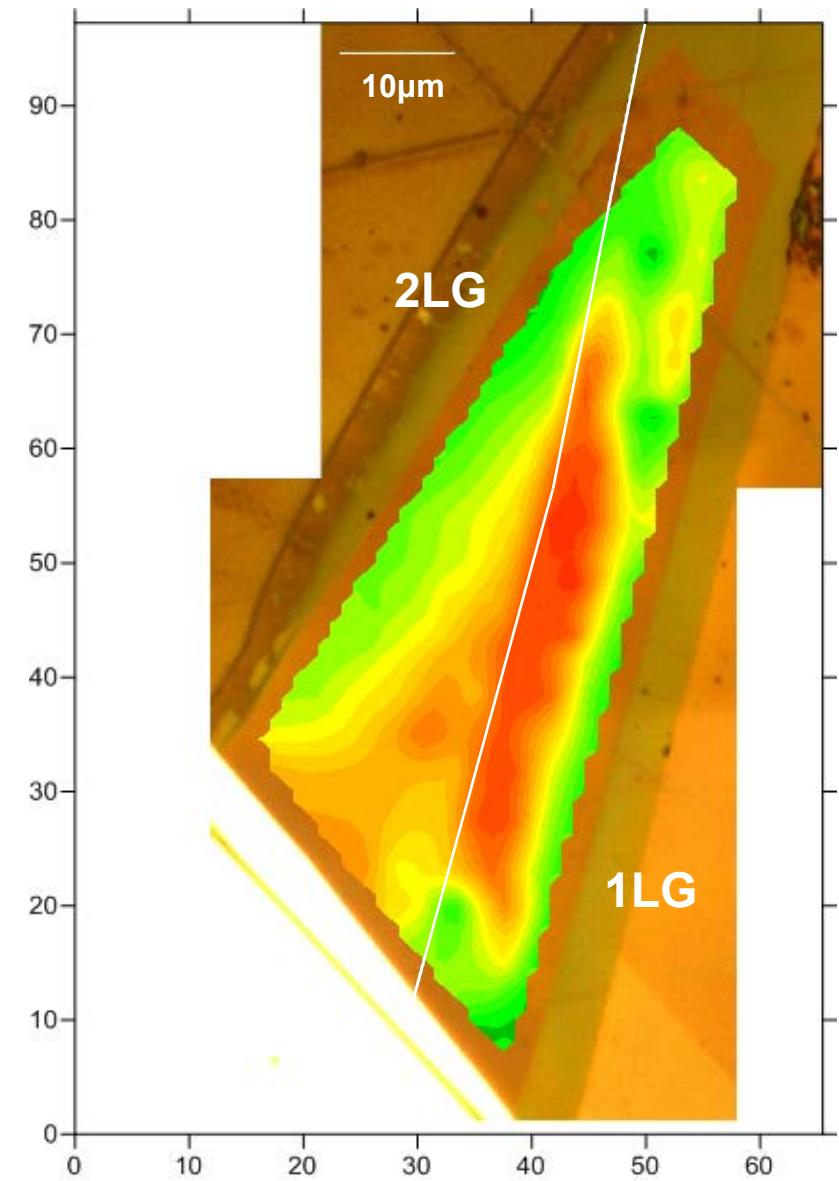
Knowing the wavenumber shift we can resolve the inverse problem i.e. to obtain the values of axial σ and/or ε in graphene composites through the above relations.

Frank et al, *Nature Comms*, 2:255, DOI 10.1038, 2011

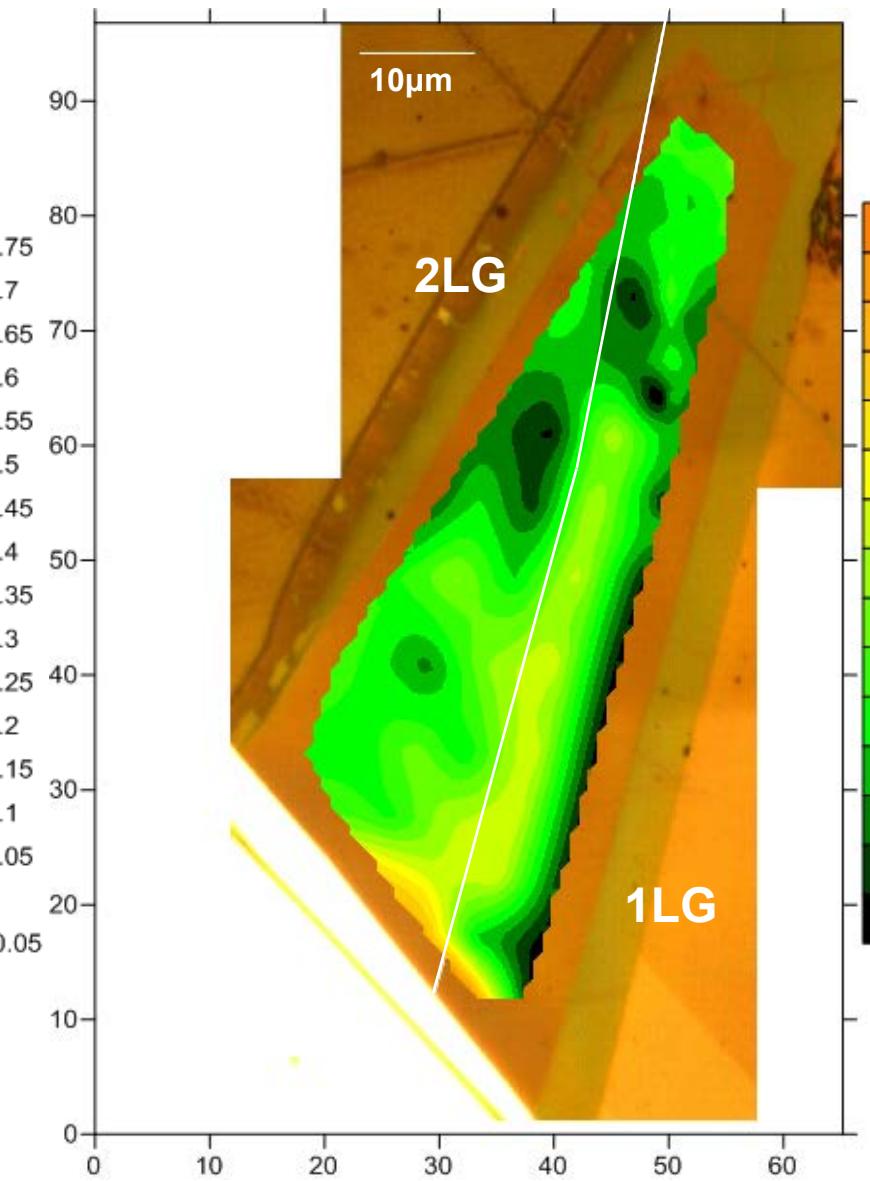


Strain maps of graphene flakes embedded into polymers

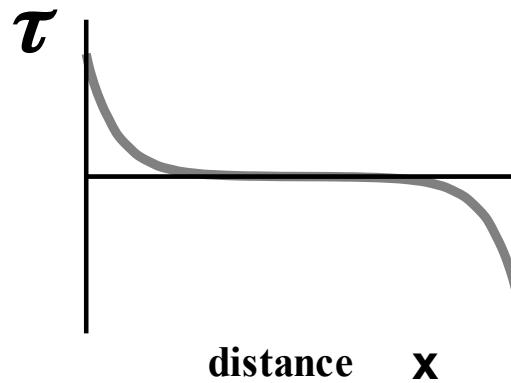
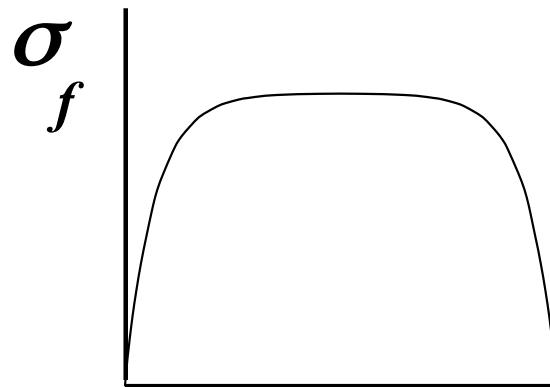
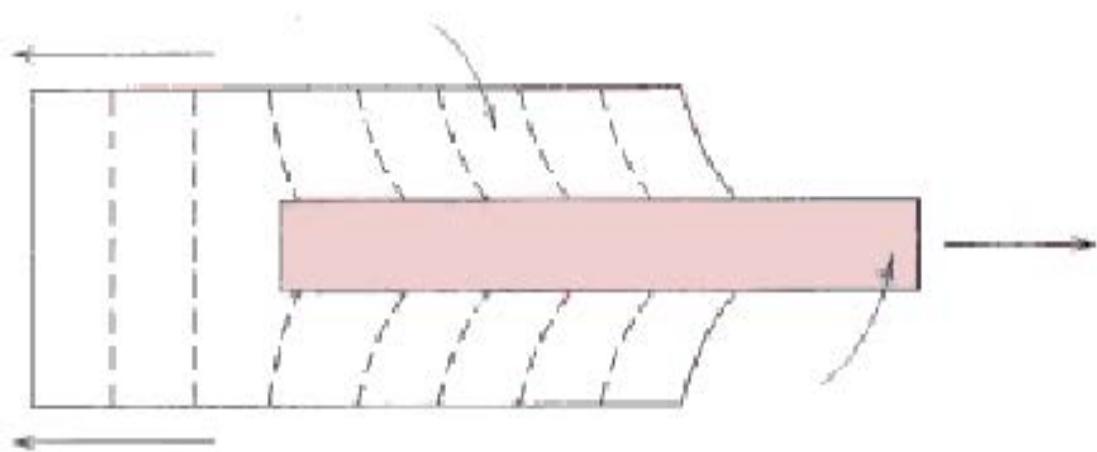
0.74%



0.0% released

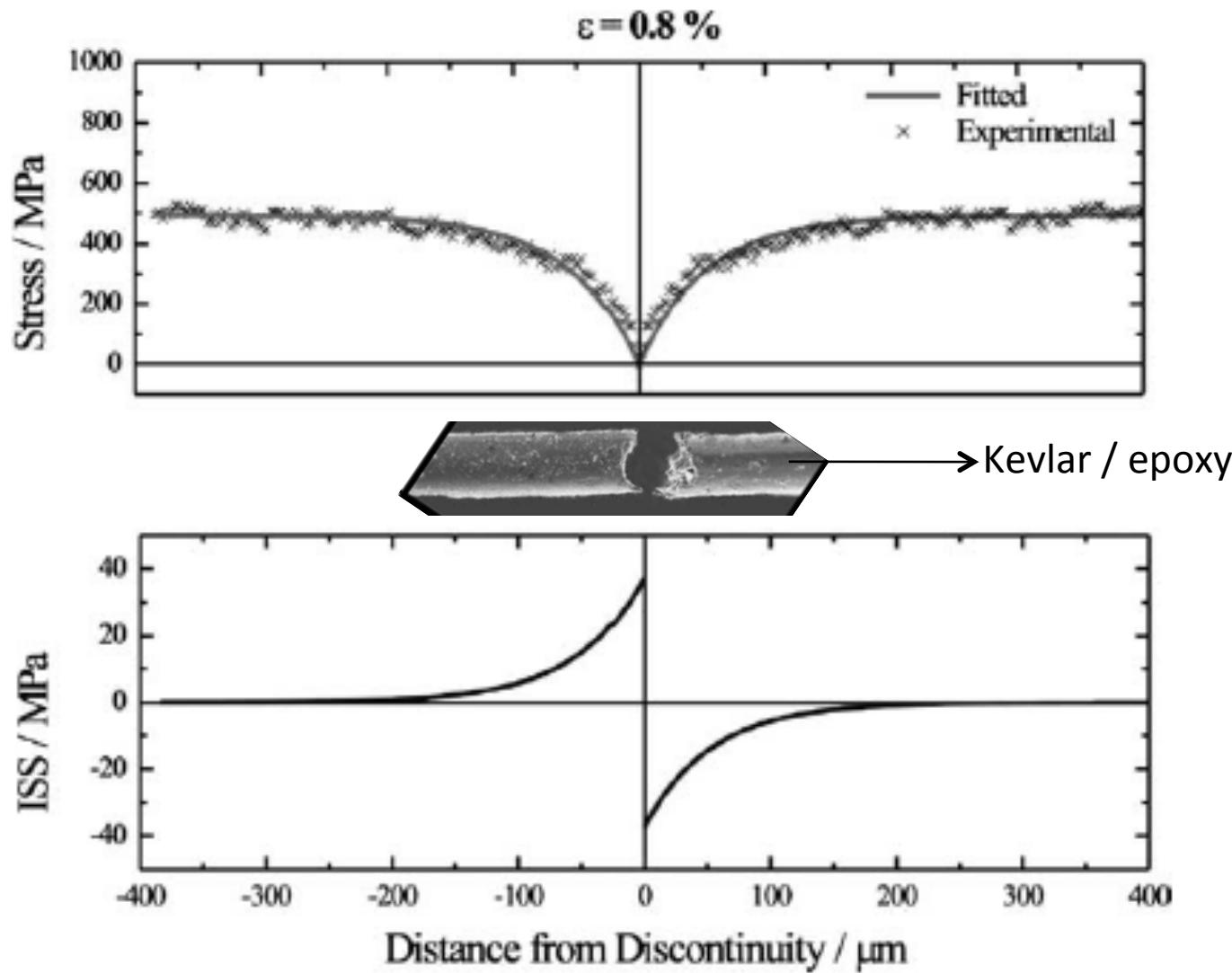


Textbook stuff: Mechanisms of Stress Transfer in Composites



Elastic transfer in polymer composites (1/2)

(shear-lag analysis)



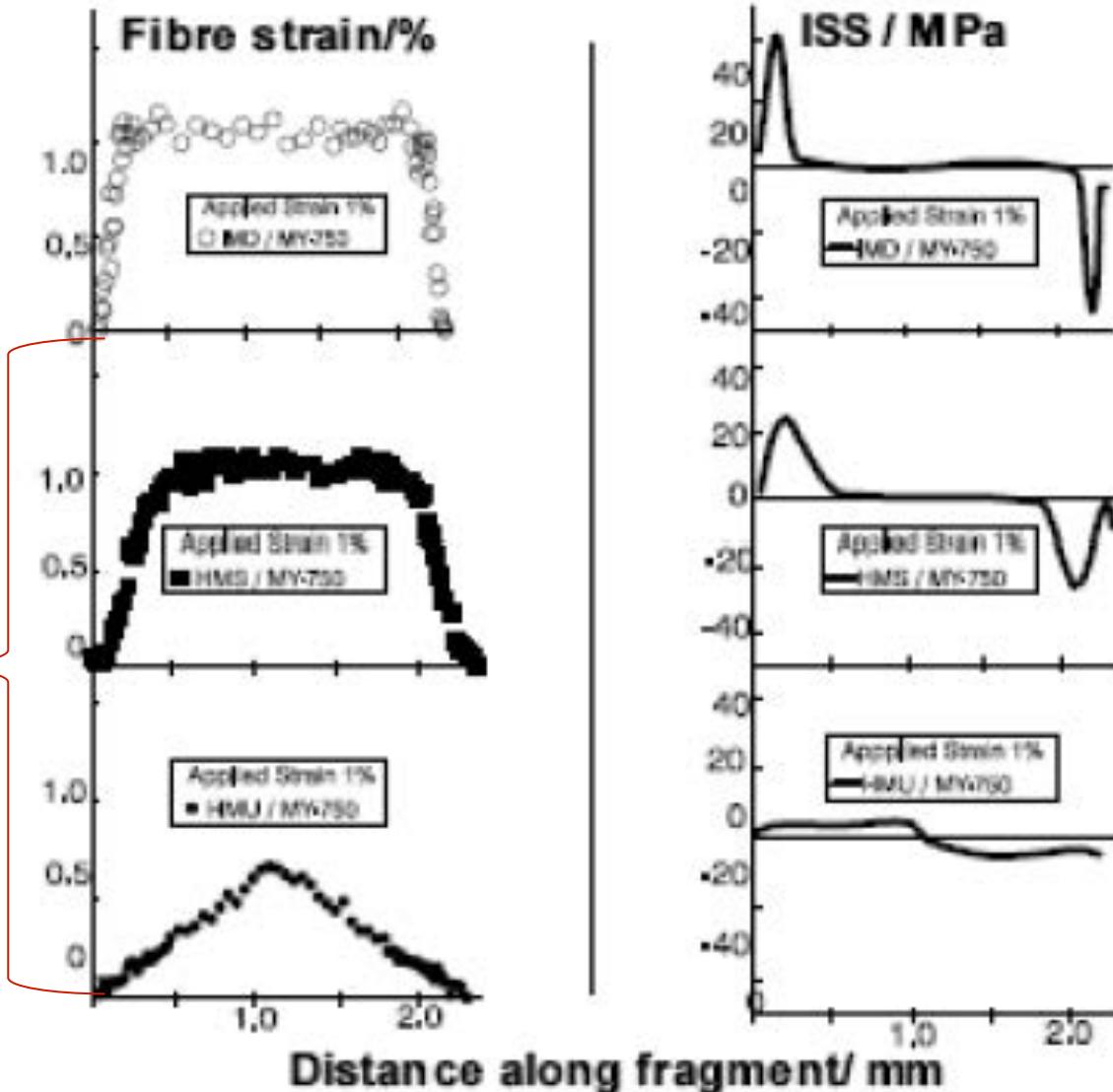
Anagnostopoulos et al, Acta Materialia, 53, 2005



Elastic transfer in polymer composites (2/2)

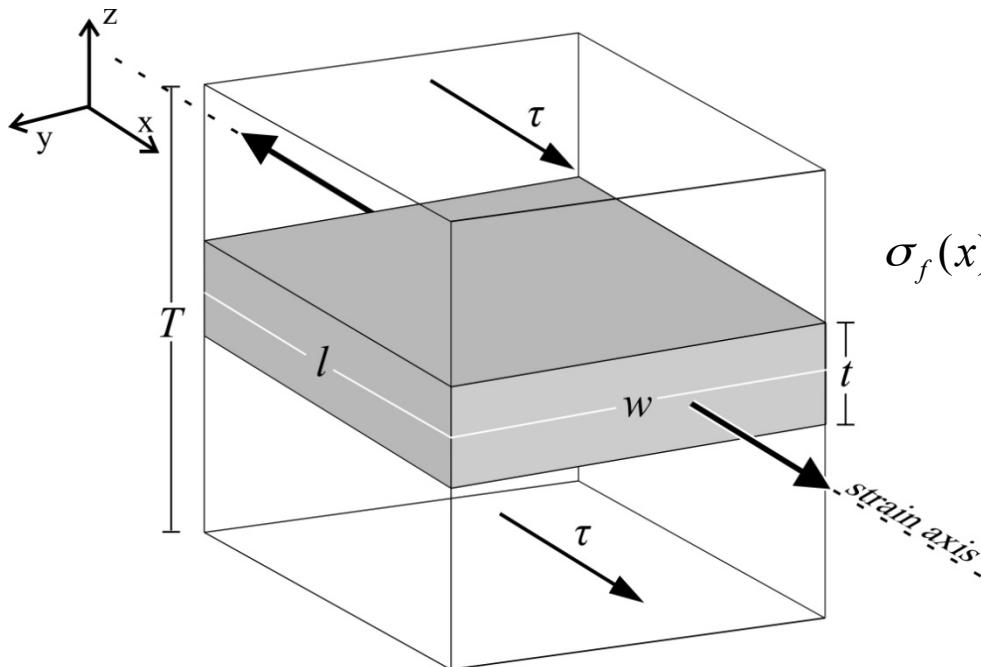
(shear-lag analysis)

Same high-modulus
carbon fibre but
different oxidative
treatment



Melanitis & Galiotis,
Proc. of Royal Soc.-A,
440 379-398, (1993)

Shear lag analysis of graphene flakes embedded into polymers

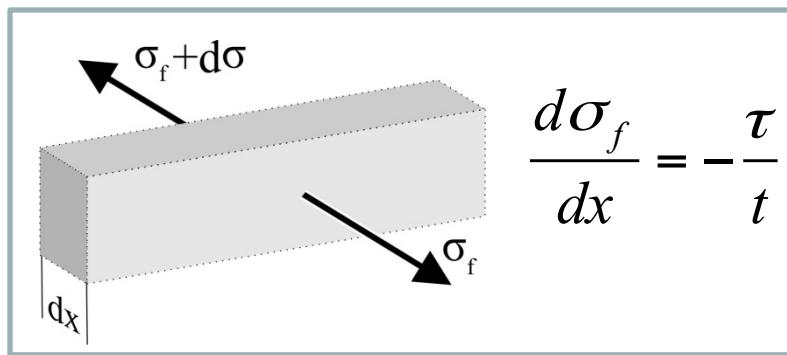


$$\frac{d^2\sigma_f}{dx^2} = \frac{H}{wt} \left(\frac{\sigma_f}{E_f} - \varepsilon \right)$$

$$\sigma_f(x) = E_f \cdot \varepsilon_\infty \cdot \left[1 - \cosh(\beta x) + \tanh\left(\frac{\beta l}{2}\right) \cdot \sinh(\beta x) \right]$$

where

$$H = \frac{wG_{m,T}}{t \ln \frac{T}{t}} \quad \text{and} \quad \beta = \frac{1}{t} \sqrt{\left(\frac{G_{m,T}}{E_f \ln \frac{T}{t}} \right)}$$



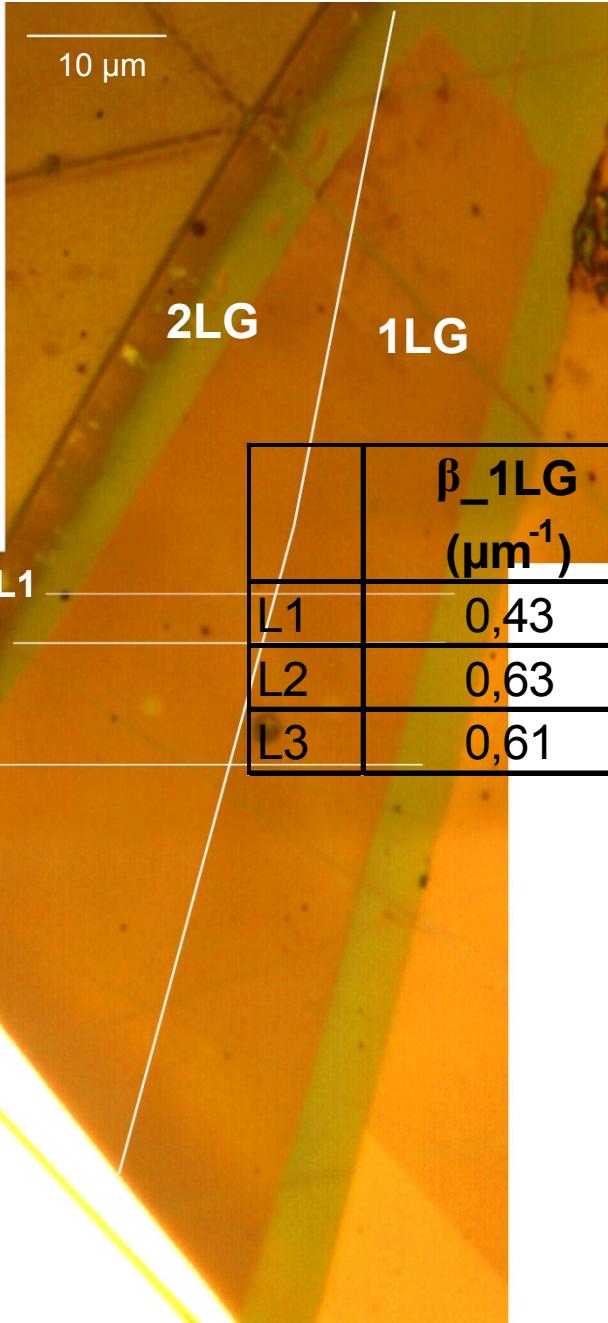
$$\frac{d\sigma_f}{dx} = -\frac{\tau}{t}$$

$$\sigma_f(x) \sim \sigma_{f,\infty} \cdot [1 - \exp(-\beta x)]$$

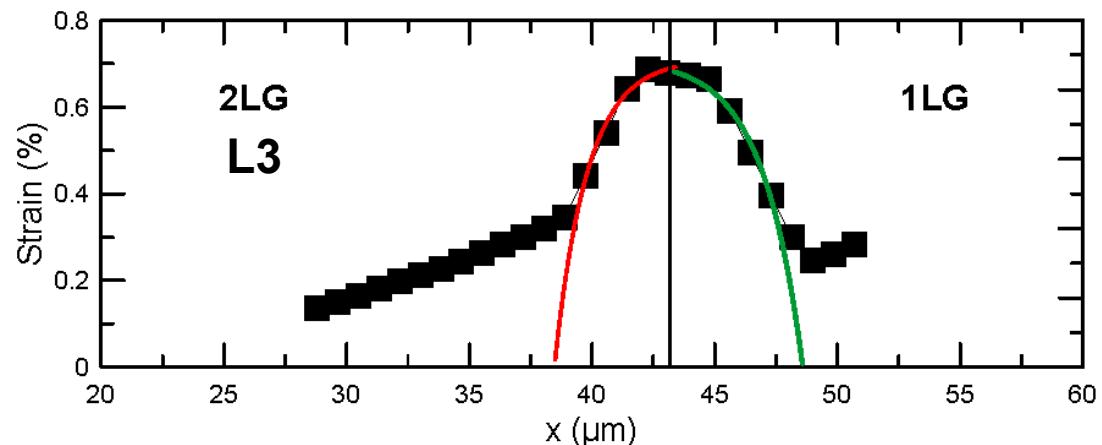
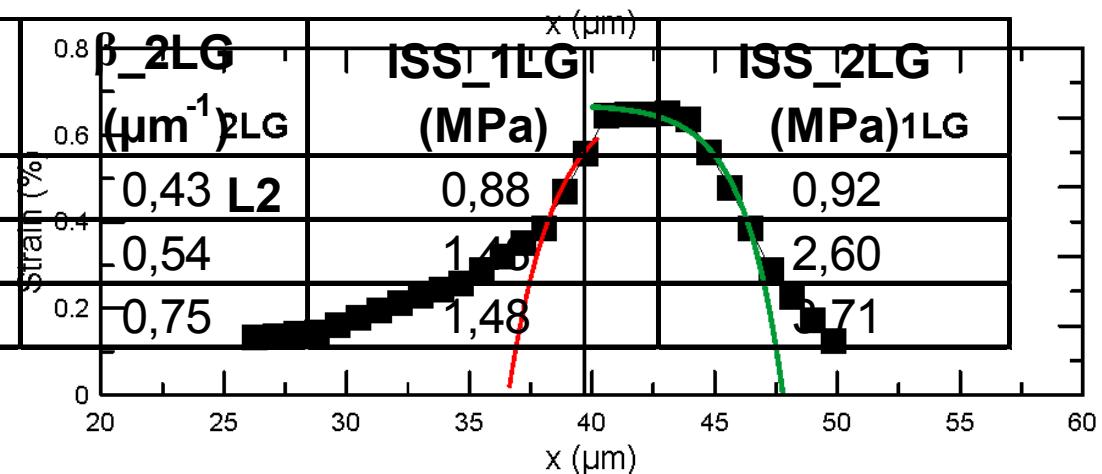
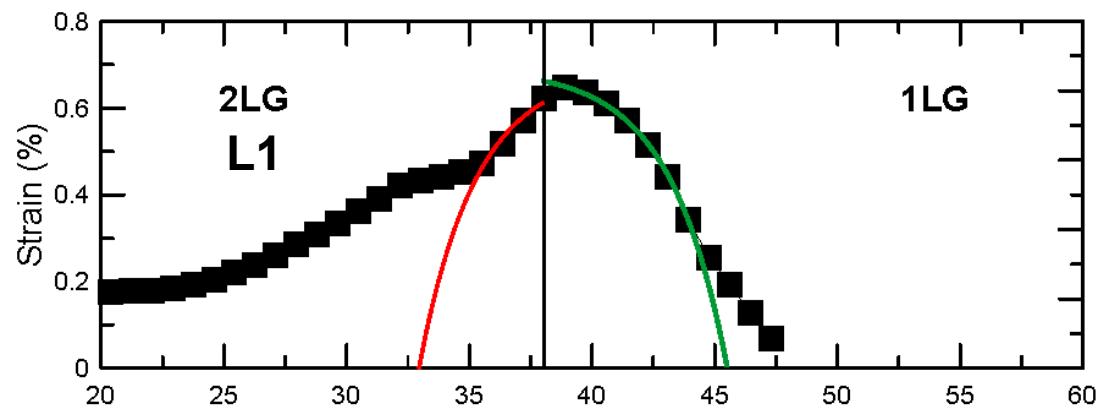
and

$$\tau \sim -te_{f,\infty} E_f \beta e^{-\beta x}$$

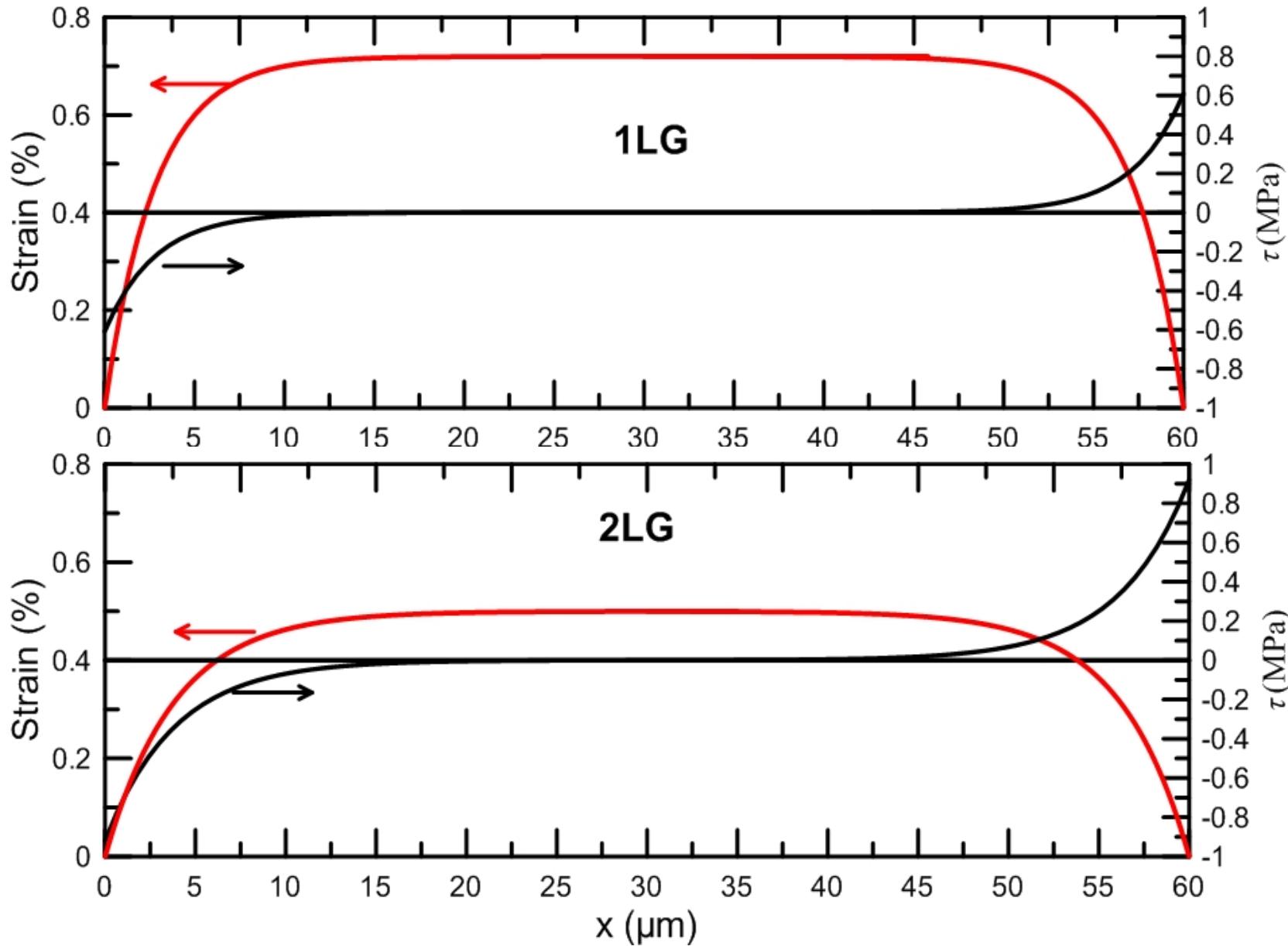
Shear lag analysis of a 1LG/ 2LG graphene flake in PMMA



	β_{1LG} (μm^{-1})
L1	0,43
L2	0,63
L3	0,61



Axial & Interfacial shear stress distributions



Conclusions

- ❖ Experiments on purely axial loading of graphene in tension have not been performed as yet.
- ❖ If no residual strain is present the phonon vs. strain relationship in tension is linear at least up to ~1.5%.
- ❖ In compression, the observed phonon relaxation is indicative of failure initiation. The obtained values of critical strain to failure for monolayer graphene agree well with Euler buckling analysis.
- ❖ The stress transfer from a polymer matrix to graphenes (1LG & 2LG) seems to proceed along macroscopic principles (shear-lag).
- ❖ Pristine graphenes exhibit poor interfacial strength in PMMA matrices. Attention should be exercised when measurements are made near the flake edges.



Acknowledgements/ Collaborations

- ❖ Dr. D. Tassis ([Univ. Patras](#))
 - ❖ Dr. A. Ferrari ([Univ. Cambridge, UK](#))
 - ❖ Prof. A. Geim ([Univ. Manchester, UK](#))
-

Financial support:

- ❖ Marie-Curie TOK
- ❖ GRAPHENE CENTRE ([FORTH](#))



Graphene bilayer under uniaxial tension – 2D band

	$\lambda = 785 \text{ nm}$		$\lambda = 633 \text{ nm}$	
	$\omega_{2\text{D}}$ [cm $^{-1}$]	$\partial\omega_{2\text{D}}/\partial\varepsilon$ [cm $^{-1}/\%$]	$\omega_{2\text{D}}$ [cm $^{-1}$]	$\partial\omega_{2\text{D}}/\partial\varepsilon$ [cm $^{-1}/\%$]
2D_{11}	2637.9 ± 2.5	-32.3 ± 6.7	2688.0 ± 2.2	-57.5 ± 7.3
2D_{12}	2621.3 ± 2.7	-55.0 ± 7.0	2671.0 ± 2.5	-57.6 ± 8.4
2D_{21}	2596.8 ± 2.8	-51.7 ± 6.2	2651.0 ± 1.3	-54.8 ± 4.4
2D_{22}	2529.3 ± 2.6	-51.8 ± 6.9	2603.1 ± 1.6	-45.6 ± 5.4

